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Spin polarization control by electric stirring: Proposal for a spintronic device

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We propose a spintronic device to generate spin polarization in a mesoscopic region by purely electric means. We show that the spin Hall effect in combination with the stirring effect are sufficient to induce measurable spin polarization in a closed geometry. Our device structure does not require the application of magnetic fields, external radiation or ferromagnetic leads, and can be implemented in standard semiconducting materials. © 2009 American Institute of Physics. [DOI: 10.1063/1.3180494]

Consider, for example, a mesoscopic conducting sample, which we will call a conducting island. In Fig. 1, four gates with a voltage signal changing with time according to the law

\[ V_k(t) = V \sin(\omega t + 2\pi k/4), \quad k = 1, \ldots, 4 \]

will induce the SE so that the electric current will flow in a preferred (clockwise or counterclockwise) direction inside the island. Let the conducting island be made of a material exhibiting the spin Hall effect \(^9-^{12}\) (SHE). Then, when circulating charge currents are excited, electrons with a certain spin polarization will deflect toward the island’s center as it is shown in Fig. 1 creating the desired spin polarization.

We take the size of conducting island to be sufficiently large to disregard the discreteness of electron energy spectrum. Depending on the screening strength, the gate voltages can create circulating currents in the whole island or only in a localized region near the boundary. The former regime is more desirable and is realizable in low or moderately doped semiconductor islands whose dimensions do not exceed several microns (see calculations below). The second regime is more relevant to heavily doped semiconductor or metal islands. By solving drift-diffusion equations near the interface between regions with zero and nonzero charge currents, one can find that spin polarization decays at a distance compa-

![FIG. 1. (Color online) Spintronic device to generate spin polarization at the center of a semiconductor island. Application of ac gate voltages induces circular charge currents in the island. SHE in such a system results in opposite spin accumulation at the center and near the boundaries of the island. Direction of the accumulated spins is along z axis and determined by the direction of gate-controlled circular charge currents.](image-url)
rable to the spin diffusion length \( L_s = \sqrt{D\tau_s} \) from the interface, where \( D \) is the charge diffusion coefficient and \( \tau_s \) is the spin relaxation time. To find substantial spin polarization near the center of the island, in the second regime, the size of the region, unperturbed by gate voltages, should not be much larger than \( L_s \). Typically, \( L_s \approx 1-10 \, \mu m \) for GaAs. Hence, due to the finite spin lifetime, the size of the conducting island can be several microns. In our numerical simulations (see below), we consider a situation when the diameter of the island is smaller than \( L_s \). In this case, substantial spin polarization at the island center is obtained.

We note that there exists another mechanism for spin polarization in our setup. Microscopically, spin-orbit coupling is described by the expression \( E_{\text{so}} = g_{\text{so}} \mathbf{L} \cdot \mathbf{S} \), where \( \mathbf{L} \) is the operator of angular momentum and \( \mathbf{S} \) is the spin operator and \( g_{\text{so}} \) is a spin-orbit coupling constant. Circulating currents carry a nonzero angular momentum, and hence lead to energy imbalance for spins with opposite orientations. This mechanism can be functional even in devices with nanoscale dimensions. However, it is expected that the SHE is the dominant mechanism for nonzero spin polarization, and, therefore, only the SHE is included in our calculations.

In the drift-diffusion approximation, the \( z \) component of spin current \( \mathbf{J}_s \) is given by

\[
\mathbf{J}_s^z = -D \nabla n_z + \lambda_{sh} \tilde{z} \times \mathbf{J}_s e,
\]

where \( n_z = n_{\uparrow} - n_{\downarrow} \) is the spin density imbalance, \( n_{\uparrow}(\downarrow) \) is the density of spin-up (down) electrons, \( \tilde{z} \) is a unit vector in the direction which is transverse to the stirring plane and \( \mathbf{J}_s \) is the charge current density. The first term in the right hand side is due to spin diffusion, and the second term describes the SHE. Experimental\(^{11}\) and theoretical\(^{13}\) studies in GaAs as well as Al samples determined the relative strength of the spin Hall current to the charge current as \( \lambda_{sh} \approx 10^{-5} - 10^{-4} \). We use a linear dependence of spin current on the charge current, which describes the extrinsic mechanism of the SHE. It is believed to dominate in \( n \)-doped GaAs.\(^{11}\)

Consider a case of a uniformly circulating electron current \( \mathbf{J}(r, \theta) = n e_{\text{so}} \omega r \hat{\theta} \), where \( n \) is the density of conducting electrons, \( \omega \) is the rotation frequency, and \( \hat{\theta} \) is the unit vector in the azimuthal direction. In the polar coordinates, the drift-diffusion equation with spin currents (1) and a phenomenological spin-relaxation term is given by

\[
\frac{\partial \mathbf{P}_s}{\partial t} = D \left[ \nabla \mathbf{P}_s + \frac{1}{r} \mathbf{r} \cdot \nabla \mathbf{P}_s \right] + \lambda_{sh} \nabla \mathbf{L}_s \cdot \mathbf{r} \frac{\partial }{\partial t} \mathbf{J}_s - \mathbf{P}_s \tau_s,
\]

where \( r \) and \( \theta \) are coordinates of a point in the polar coordinate system. Equation (2) has a simple stationary solution that describes a rotating electron gas in a conductor of infinite diameter and

\[
P_z = 2 \omega n \lambda_{sh} \tau_s.
\]

It cannot be valid near the boundary of a finite system, however, it provides a good estimate of the spin polarization far away from the boundary inside a sufficiently large structure. Taking \( \tau_s \approx 10^{-8} \, s \), \( \lambda_{sh} \approx 10^{-4} \), and \( \omega \approx 10^9 \, s^{-1} \) we find that \( P_z \approx n 10^{-3} \), i.e., about 0.1% of electrons will be spin polarized near the center of the structure.

The application of an ac gate voltage is akin to the application of a rotating electric field. At optical frequencies, such a field is known to induce transitions between the va-

![Figure 2](image-url)

**FIG. 2.** (Color online) Distributions of (a) spin polarization \( p_z \), (b) charge current density \( \mathbf{J}_s e \), and (c) potential calculated in a system containing a circular semiconductor island of radius \( R = 1 \, \mu m \) subjected to a rotating electric field. (a) and (b) were found as an average over a field rotation period \( T \), while (c) is an instantaneous potential profile at \( t = 5 \, ns \). The following values of parameters were used: \( n = 10^{15} \, cm^{-3} \), \( \tau_s = 20 \, ns \), \( \lambda_{sh} = 10^{-3} \), \( \mu = 8500 \, cm^2/(V \, s) \), \( L_s = 7 \, \mu m \), \( E_0 = 5 \, kV/cm \), and \( T = 1 \, ns \). \( E_0 = 5 \, kV/cm \) corresponds to 1 V voltage drop over 2 \( \mu m \) (diameter of the island).

ence and conduction bands of semiconductors, creating spin polarization. In our device, this field rotates with a microwave frequency and cannot induce spin polarization via the conventional mechanism. It can, however, excite circulating currents.\(^{14}\)

We solve numerically a system of two-component drift-diffusion equations supplemented by the Poisson equation. Our numerical scheme is similar to those used in Ref. 15 with the only difference that now we are solving equations in two dimensions. The Poisson equation is solved in a larger area enclosing the conducting island with the boundary condition that the potential at the boundary of the larger area is presented by the rotating electric field. The rotating electric field can be written as \( \mathbf{E} = E_0 \cos(\omega t) \hat{x} \pm E_0 \sin(\omega t) \hat{y} \), where \( E_0 \) and \( \omega \) are the electric field amplitude and angular frequency, \( \hat{x} \) and \( \hat{y} \) are unit vectors in the \( x \) and \( y \) directions, and \( \pm \) corresponds to a \( \sigma_z \) circular polarization.

Figure 2 shows a representative result of our calculations. Here, we consider a moderately doped GaAs island of a circular shape. At the selected value of electron density \( n = 10^{15} \, cm^{-3} \), the electric field penetrates deep inside the island creating circulating currents which are not limited to the surface [Fig. 2(b)]. The spin polarization calculated as \( p_z = \langle n_{\uparrow} - n_{\downarrow} \rangle / \langle n_{\uparrow} + n_{\downarrow} \rangle \), where \( \langle \ldots \rangle \) denotes averaging over the rotating field period, has a magnitude \( \sim 8 \times 10^{-4} \) at the center.
In conclusion, we proposed a spintronic device that generates a spin polarization in a localized region of a semiconductor by purely electric means. Importantly, our device structure does not require the application of magnetic fields, external radiation or ferromagnetic leads, and can be implemented in standard semiconductor materials. The novelty of our approach is in considering the combination of two effects, namely the SHE and the stirring effect. Our numerical simulations confirm that the induced spin polarization is sufficiently strong to be observable by the Kerr rotation technique. Our spintronic device can be used to generate spin-polarized currents or to control the magnetization of a nanomagnet placed at the center of the conducting island, e.g., by doping Mn ions.

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![Graph](image)

**FIG. 3.** (Color online) Spin polarization at the island’s center at different values of the field rotation period $T$. Inset: spin polarization at the island’s center at different values of electron density $n$ at $T=1$ ns. Here, we used the same values of all other parameters as in Fig. 2.

In Fig. 3, we plot the spin polarization magnitude at the island center as a function of the rotating field period and electron density (inset). When we start to decrease $T$ from 5 ns, $P$ increases first as is expected from Eq. (3), and has a maximum at $T \approx 0.5$ ns and then decreases. This decrease is possibly related to the resonance nature of circulating current excitation or strong spin densities mixing in highly nonequilibrium environment. An increase of the electron density results in a decrease of the spin polarization (see the inset in Fig. 3) mainly because at higher electron densities, the circulating currents are limited to the surface regions. We note that in a real setup, this effect should be less important because the finite viscosity of the electron fluid as well as the finite thickness of the island are not captured by our two-dimensional calculations. Then, when a finite thickness of the island is taken into account, the exponential three-dimensional screening reduces to a power-law type and the electric field penetrates deeper into the island creating stronger SE.