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Dynamic path bifurcation for the Beckmann reaction: observation and implication

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Dynamic path bifurcation for the Beckmann reaction: observation and implication

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The reaction of oximes to amides, known as the Beckmann rearrangement, may undergo fragmentation to form carbocations + nitriles instead of amides when the cations have reasonable stability. The reactions of oxime derivatives of 1-substituted-phenyl-2-propanones and 3-substituted-phenyl-2-butanones in aqueous solvents gave both rearrangement and fragmentation products, the ratio of which was dependent on substituents. Transition state (TS) optimizations and intrinsic reaction coordinate (IRC) calculations for the reaction of 1-phenyl-2-propanone oximes showed that there is a single TS for each substituted compound. The IRC path from the TS either led to a rearrangement product or a fragmentation product depending on the substituent; the IRC path changes from rearrangement to fragmentation when substituent X becomes more electron donating. *Ab initio* dynamics simulations were found to follow the IRC path for X = *p*-NH₂ and *p*-MeO giving fragmentation products, and almost so for X = *p*-NO₂ giving the rearrangement products. However, in a borderline case where X is less donating than *p*-MeO or less withdrawing than *p*-NO₂, the trajectories did not follow the minimum energy path on the potential energy surface, but gave both rearrangement and fragmentation products directly from the single TS. This is a novel example of path bifurcation for a closed shell anionic reaction. It was concluded that a reactivity-selectivity argument based on the traditional TS theory may not always be applicable even to a well-known textbook organic reaction.

1 Introduction

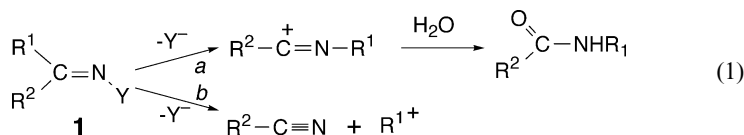
When an organic reaction yields two products, the kinetic selectivity is viewed as arising from the relative rates of the two concurrent pathways leading to the two products. Accordingly, high-selective synthetic reactions have often been designed to stabilize the transition state (TS) of the main reaction relative to that for a minor product. To study organic reaction mechanisms, it has become a common practice to use molecular orbital (MO) methods and to calculate TS structures and in some cases potential energy surfaces (PESs). Although MO calculations have achieved numerous contributions in the field of mechanistic organic chemistry, it should be noted that the calculated structures, energies and reaction pathways are at 0 K, and therefore information obtained from MO calculations may not directly be related to experimental observations at a finite temperature.

It has been increasingly recognized by means of molecular dynamics (MD) simulation studies that dynamics effects play a crucial role in controlling the reaction

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mechanism for mechanistically borderline reactions.¹ In a pioneering study reported in 1985, Carpenter demonstrated a possible role of dynamics effect in chemical reactions. He showed by using a model PES that when two symmetrical products were formed from a common intermediate through isoenergetic barriers, the two products might be obtained in unequal amounts depending on how the common intermediate was formed.² This was a new interpretation of an old idea, a memory effect. Since then, dynamics effects have been claimed to play an important role in various reactions. It appears in different ways, such as nonstatistical barrier recrossing,³ nonstatistical product distribution,⁴ shallow minimum skip on the intrinsic reaction coordinate (IRC),⁵ non-IRC path,^{6–8} and path bifurcation.^{9,10} All these results suggested that the mechanism of these reactions could not be defined by the reaction paths on the PES and by the traditional TS theory.

The Beckmann rearrangement is a textbook reaction, in which oximes under acidic conditions or those with an appropriate leaving group (Y) under solvolytic conditions give amide *via* intramolecular rearrangement (path *a* in eqn (1)). Oximes have been known to give fragmentation products when the R¹ group, which is located *anti* to Y, is stabilized as a cation by an adjacent group, such as O,¹¹ S,¹² N,¹³ Si,¹⁴ and CH=CHR.¹⁵ Grob *et al.* reported in 1964 that the reaction of ketoxime tosylate (**1**, Y = OTs) in 80% aq. EtOH gave two types of products and that the percentage of the fragmentation product (F/(F + R)) increased when the R¹ group became better stabilized as a cation (R¹ = CHPh₂ > *t*-Bu > *i*-Pr).¹⁶ On the other hand, the reactivity was found not to follow the same order (R¹ = *t*-Bu > *i*-Pr > Ph > Et > CHPh₂). Thus, the product selectivity and the reactivity were controlled in different steps.



Preliminary molecular orbital (MO) calculations from our laboratory have shown that the reactions of ring-substituted 1-phenyl-2-propanone oxime derivatives (**1**, R¹ = XC₆H₄CH₂, R² = CH₃, Y = OH₂⁺) gave either a fragmentation or a rearrangement product depending on the substituent through a single TS on the PES.¹⁷ The IRC reached the fragmentation product region for X = *p*-MeO, whereas it gave the rearranged product for X = *p*-Me, H, *p*-CN, *p*-NO₂. Thus, the reaction mechanism switched through the variation of the nature of a single TS rather than the variation of relative feasibility of concurrent reactions.

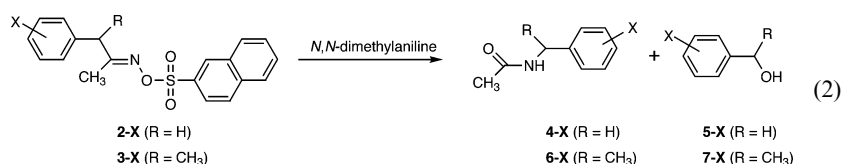
In this paper, the results of a combined experimental and computational study will be discussed, with stress on the dynamics effect on the reaction mechanism. In particular, possible occurrence and the origin of path bifurcation will be analyzed.

2 Results and discussion

Experimental results

The reactions of ring substituted 1-phenyl-2-propanone oxime 2-naphthalenesulfonates (**2-X**) and 3-phenyl-2-butanone oxime 2-naphthalenesulfonates (**3-X**) were examined in aq. MeOH and aq. MeCN at 25 °C (eqn (2)). The reaction of **2-H** in aq. MeOH gave the corresponding amide (**4-X**) as a major product, together with small amounts of benzyl alcohol (**5-X**) and benzyl ether. Thus, the major product was from the rearrangement process. In order to analyze closely the correlation between the product ratio and the overall reactivity, we chose aq. MeCN as the solvent system, where the product composition was simple with only amide

(rearrangement) and alcohol (fragmentation) as each type of the product and the reaction rates were conveniently measured by a spectroscopic method. The rates and product distributions of the reactions of **2-X** and **3-X** were determined in aq. MeCN at 25 °C. The first-order rate constants are summarized together with the product ratio in Table 1. Although the experimental study is still in a preliminary stage in terms of the number and the type of substituent, the data in Table 1 clearly shows that substrates **3-X**, especially those with electron-donating substituents, yielded a significant amount of fragmentation product in addition to the rearrangement product. Despite the difference in the product composition, the relative reactivities for the two systems (**2-X** and **3-X**) gave reasonably good linear correlation (Fig. 1).



There are three possible explanations for the results. First, the two products are formed *via* competitive pathways as in eqn (1). This explanation is unlikely, since this requires the two TSs to have similar electron demand, despite the electron demand in the intermediates being very different. It is also not consistent with the preliminary computational result that there was only one TS on the PES for protonated 1-phenyl-2-propanone oxime (**1**, $\text{R}^1 = \text{XC}_6\text{H}_4\text{CH}_2$, $\text{R}^2 = \text{CH}_3$, $\text{Y} = \text{OH}_2^+$) leading to either the fragmentation or the rearrangement product.¹⁷ In the second interpretation, these reactions go through a TS to give the rearranged intermediate ($\text{CH}_3\text{C}^+ = \text{NCHRAr}$, $\text{R} = \text{H}$ or Me), which may afford amide upon hydrolysis or $\text{MeCN} + \text{benzylic cation}$ upon N-C bond cleavage. Thus, the rate-determining and product-determining steps are different steps with a common intermediate for the two products. It is difficult to eliminate the possibility completely by experiment, but this explanation requires that the N-C bond cleavage in the cationic intermediate is competitive with the attack of solvent water on the cation. The former step is endothermic at least in the gas phase (8.7 (20.8) kcal mol^{-1} in free energy for **2-H** at HF/6-31G* (MP2/6-31G*)), whereas the latter step is likely to be exothermic and very fast in aq. solvent. Finally, the third interpretation is that the reactions proceed through a single TS and the path bifurcates afterwards to give the two products. Recently, path bifurcation phenomena have been reported in several reactions,^{9,10} most of which involve open-shell species. It is important to

Table 1 First-order rate constants and the product ratios at 25 °C for the reactions of substituted 1-phenyl-2-propanone oxime 2-naphthalenesulfonates (**2-X**) in 80% (v/v) aq. MeCN and of substituted 3-phenyl-2-butanone oxime 2-naphthalenesulfonates (**3-X**) in 90% (v/v) aq. MeCN

X	2-X		3-X	
	$k/\times 10^{-5} \text{ s}^{-1}$	R/(F + R) ratio ^a	$k/\times 10^{-4} \text{ s}^{-1}$	R/(F + R) ratio ^a
<i>p</i> -CH ₃	241 ± 4	92.4	114	46.7
H	81.5 ± 17	100.0	40.7	78.7
<i>p</i> -Cl	28.2 ± 16	nd ^b	15.4	79.6
<i>m</i> -Cl	10.1 ± 0.1	nd ^b	5.52	94.2
<i>p</i> -CF ₃	4.52 ± 0.05	nd ^b	2.46	98.4

^a The percentage of the rearrangement product over the total product. ^b Not determined.

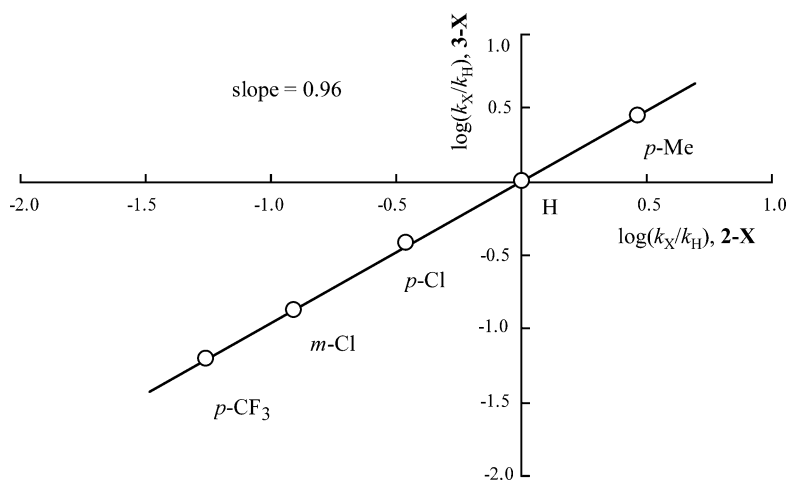


Fig. 1 Correlation between relative reactivities for 2-X and 3-X in aq. MeCN at 25 °C.

examine the possible bifurcation for the well-known textbook reaction with closed shell species.

MO calculations

In the present calculations, the acid-catalyzed reactions of substituted 1-phenyl-2-propanone oximes (**8-X**) were examined in detail (eqn (3)), in which oximes give protonated intermediates (**Int**) and then lead to the fragmentation or the rearrangement product. We used protonated water trimer as the proton source (YH^+ in eqn (3)) for the initial protonation of oximes, but the choice of the proton source does not affect the substituent effect and the reaction mechanism. At both HF/6-31G* and MP2/6-31G* levels, a single TS was optimized for the N–O bond fission process for each substituted derivative. The calculated TS structures for substrates with strongly electron-donating (**8-p-NH₂**) and electron-withdrawing (**8-p-NO₂**) substituents are shown in Fig. 2, which shows that the both TS structures look similar. The activation energies and selected geometrical parameters of the TSs are summarized in Table 2. The activation barrier is lower for a substrate with a more electron donating substituent, as expected for the N–O bond heterolysis. The TS structure varies smoothly from a more product-like to a more reactant-like one when the substituent varies from electron-withdrawing NO₂ to electron-donating NH₂, which is consistent with the Leffler–Hammond principle.¹⁸ The

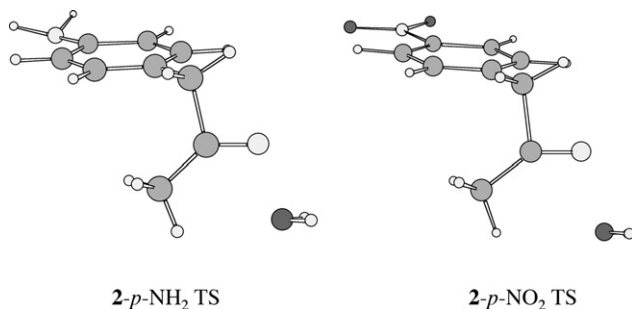


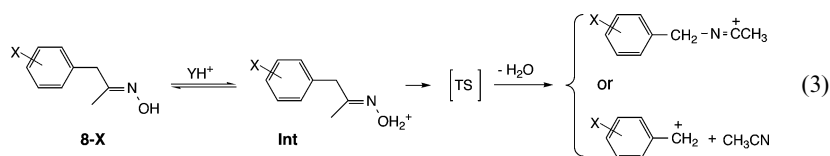
Fig. 2 TS structures for **8-X** (X = *p*-NH₂ and *p*-NO₂) at MP2/6-31G*.

Table 2 Calculated activation energies at HF/6-31G* and at MP2/6-31G*, and selected TS geometrical parameters at MP2/6-31G* for the reactions of **8-X**

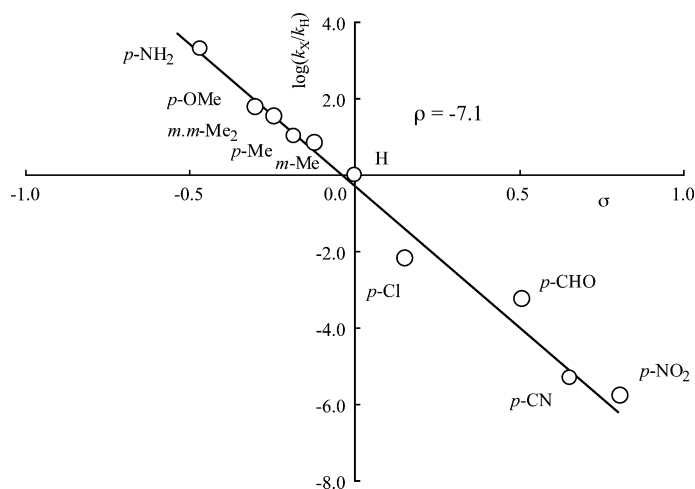
X	Activation energy ^{a,b}	Activation energy ^{a,c}	R_{C-C}^d	θ_{CCN}^e	R_{N-O}^f
<i>p</i> -NH ₂	13.5 (13.6)	22.9 (24.3)	1.604	102.9	1.852
<i>p</i> -MeO	15.3 (15.5)	25.0 (26.5)	1.614	101.5	1.880
<i>p</i> -Me	15.8 (15.7)	26.0 (27.3)	1.623	100.0	1.911
<i>m,m'</i> -Me ₂	15.4 (15.2)	25.4 (26.5)	1.622	99.8	1.914
<i>m</i> -Me	16.0 (16.3)	26.3 (27.5)	1.626	99.3	1.923
H	16.8 (16.8)	27.4 (28.7)	1.629	98.9	1.930
<i>p</i> -Cl	20.3 (20.1)	30.4 (31.6)	1.636	98.6	1.937
<i>p</i> -CHO	21.5 (21.3)	31.9 (33.0)	1.639	97.6	1.953
<i>p</i> -CN	24.5 (24.1)	34.7 (35.8)	1.647	96.8	1.968
<i>p</i> -NO ₂	26.0 (25.4)	35.3 (36.4)	1.650	96.1	1.978

^a ΔH^\ddagger (ΔG^\ddagger) in kcal mol⁻¹ with respect to separated reactants. ^b Energies at HF. ^c Energies at MP2. ^d Distance between benzylic carbon and imino carbon in Å. ^e In degrees. ^f In Å.

smooth TS variation itself is suggestive of the same reaction mechanism for all substituted substrates.



Relative activation enthalpies (ΔH^\ddagger) in Table 2 were converted to $\log(k_X/k_H)$ at 298 K, and were plotted against the Hammett σ constants in Fig. 3. Here, we used enthalpies, because the size of the entropy and hence the free energy depend

**Fig. 3** Hammett plots for the reactions of **8-X**. Relative reactivities at 298 K were calculated with the MP2/6-31G* enthalpies.

much on low frequencies, which are less reliable than higher frequencies, especially for compounds with weak interactions such as TS. The use of free energy (ΔG^\ddagger) gave similar correlations with more scattered points. The σ values were taken from gas-phase experiments.¹⁹ The linear Hammett plots in Fig. 3 may be taken to suggest that the mechanism does not change as a function of substituent.

Although the TS structures and their energies appeared to suggest a common reaction mechanism for all substituted derivatives, IRC calculations revealed that the reaction mechanism varies depending on the electronic nature of the substituent as shown in Fig. 4. Here, the abscissa is the reaction coordinate and the ordinate is the atomic distance between the benzylic carbon and the nitrogen, and only the IRC traces toward the products are shown. The C–N distance is shorter at the TS than at the reactant (2.184 Å vs. 2.286 Å, for X = H) and becomes as small as 1.4 Å in the rearrangement product, whereas it becomes larger than 2.5 Å in fragmentation. It can be seen that the IRC for substrates with an electron-withdrawing substituent reached the rearrangement product state with a short C–N distance. On the other hand, the IRC for substrates with an electron-donating substituent led to the product with a long C–N distance. The two computational methods (HF and MP2) gave qualitatively the same results, in that the path switched from rearrangement to fragmentation when substituent became more electron donating. Overall, it is clear in Fig. 4 that the IRC pathway varies continuously with the substituent, from clear rearrangement (*p*-NO₂, *p*-CN and *p*-CHO) through borderline fragmentation-rearrangement (X = *p*-Cl, H, *m*-Me, *m,m'*-Me₂, and *p*-Me) to fragmentation (*p*-MeO and *p*-NH₂ at MP2) and that the product is either one of the two for each derivative, even for the borderline cases. As a result, despite the fact that the nature of the TS in terms of structure and energy varies smoothly with substituent, the reaction product and the reaction mechanism on the PES exhibit a sharp change as a function of the substituent.

The present findings indicate that mechanistic variation is not necessarily accompanied by a sharp variation in reactivity and TS structure, and hence experimentally observable quantities, such as relative reactivities (Hammett equation) and kinetic isotope effects, which are commonly considered to be useful means to detect a change in a reaction mechanism, may not always be useful.

Trajectory calculations

Direct-MD calculations starting at the TS of each substituted substrate (**8-X**) were carried out in order to see how the mechanism changes with substituent. Three methods, HONDO, PEACH and Gaussian (G03), were used, and a total of 810 trajectories were obtained at the HF/6-31G* level. In addition to trajectories that go back to the reactant (protonated oxime) region, three types of productive

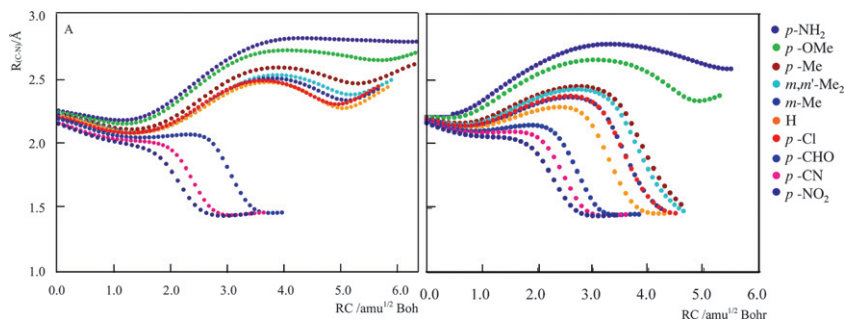


Fig. 4 IRC pathways for reaction (3) at (A) HF/6-31G* and (B) MP2/6-31G*.

trajectories were observed: type R leading directly to the rearrangement region, type F leading directly to the fragmentation region, and type $R \rightarrow F$, which initially goes to the rearrangement region and then leads to the fragmentation product. Representative trajectories are illustrated in Fig. 5, in which the abscissa is the N–O atomic

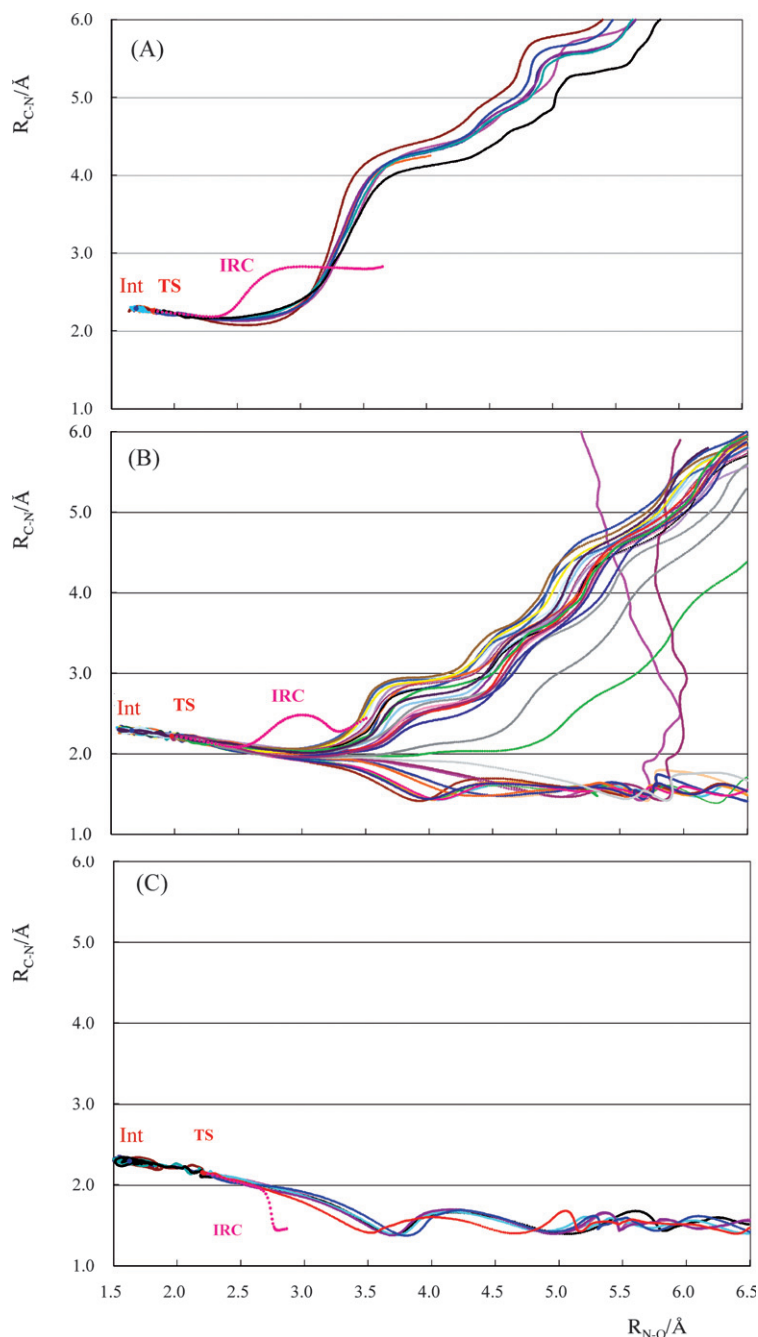


Fig. 5 Two-dimensional plots of MD trajectories obtained by PEACH at the initial kinetic energy of 50 K: (A) 8-*p*-NH₂, (B) 8-H, and (C) 8-*p*-NO₂.

distance and the ordinate is the atomic distance between the benzylic carbon and the nitrogen. The results for **8-*p*-NH₂** in Fig. 5A clearly indicate that all trajectories directly lead to the fragmentation region (type F). In Fig. 5C are shown the trajectories for **8-*p*-NO₂**, all of which are type R. Thus, trajectory calculations for these two substrates gave results that agreed with the IRC calculations. In contrast, simulations with one of the borderline substrates (**8-H**) gave both type F and R trajectories as illustrated in Fig. 5B.

Table 3 summarises the results of trajectory calculations for 10 substituted derivatives. There were trajectories that went back to the reactant region but afterward moved to the product regions, and these were counted as productive runs in Table 3. The type R → F trajectories were counted as type R. It was found that the three methods gave qualitatively the same results. Substrates with an electron-donating substituent led to the fragmentation region exclusively, whereas those with an electron-withdrawing substituent gave predominantly the rearranged products. For the borderline substrates, trajectories from their respective TS gave both fragmentation

Table 3 Summary of the trajectory calculations

X	IRC ^a	Appl.	<i>n</i> ^b	R ^c	F ^d	R% ^e	R → F ^f
<i>p</i> -NH ₂	F	G03	10	0	10	0	0
		HONDO	nd ^g	nd	nd		
		PEACH	10	0	8	0	0
<i>p</i> -MeO	F	G03	15	0	15	0	
		HONDO	10	0	9	0	0
		PEACH	10	0	9	0	
<i>p</i> -Me	F	G03	20	3	17	15	0
		HONDO	20	0	19	0	0
		PEACH	20	0	13	0	
<i>m,m'</i> -Me ₂	F	G03	20	5	15	25	3
		HONDO	nd	nd	nd		
		PEACH	20	1	12	8	
<i>m</i> -Me	F	G03	30	12	18	40	8
		HONDO	nd	nd	nd		
		PEACH	30	4	20	17	
H	F	G03	50	12	36	25	5
		HONDO	50	6	24	20	1
		PEACH	50	13	21	38	10
<i>p</i> -Cl	F	G03	50	9	39	19	1
		HONDO	50	9	23	28	0
		PEACH	50	10	23	30	3
<i>p</i> -CHO	R	G03	50	34	16	68	4
		HONDO	50	29	3	91	0
		PEACH	50	32	1	97	0
<i>p</i> -CN	R	G03	30	22	8	73	5
		HONDO	20	20	0	100	0
		PEACH	20	11	0	100	
<i>p</i> -NO ₂	R	G03	15	14	1	93	2
		HONDO	10	8	0	100	0
		PEACH	10	6	0	100	

^a IRC leading to rearrangement (R) or fragmentation (F) product. ^b Number of trajectories.

^c Number of trajectories that lead to the rearrangement region. ^d Number of trajectories that lead to the fragmentation region. ^e %Rearrangement 100(R/(R + F)). ^f Number of trajectories that first go to the rearrangement region and then lead to the fragmentation product region.

^g Not determined.

and rearrangement products directly. The results with G03 showed more mixture than those with other two methods, probably due to the difference in the initial sampling procedure. The fact that the same trends were observed qualitatively indicates that the present results are not due to any artifact in the simulation methods.

Path bifurcation. The fact that the trajectories starting from a single TS led to two products indicates that the reaction path bifurcates dynamically on the way from the TS to the products, despite the IRC path on the PES being connected to either one of the two products for each borderline substrate. The path bifurcation violates the TS-based reaction theory and thus suggests that a TS of a given character may have only limited significance with respect to the actual mechanism.

The effect of kinetic temperature on the trajectory was examined by running the simulations at 10 K for three borderline substrates with PEACH. In contrast to the higher temperature trajectories, in which the three substrates gave a mixture of type F and R trajectories as mentioned above, **8-H** (20 productive runs) and **8-p-Cl** (20 productive runs) gave only type F trajectories, and **8-p-CHO** (20 productive runs) gave only type R trajectories. Thus, the low temperature trajectories followed the IRC paths. It is clear that the dynamic path bifurcation is kinetic energy dependent.

Comparison of MD trajectories in Fig. 5 with IRC revealed that trajectories initially following the IRC paths start to deviate at $R_{N-O} = 2.5$ Å in type F (Fig. 5A) and 2.7 Å in type R (Fig. 5C) from IRC in such a way that the N–O bond cleavage continues to occur ahead of the benzyl group departure (type F) or the C–N bond formation (type R). Thus, both the fragmentation and rearrangement processes are concerted on the PES, whereas they are rather asynchronous two-stage processes in dynamics. The phenomenon is reminiscent of formally concerted and dynamically two-stage reactions reported in the literature.^{7,8,20}

Origin of bifurcation. Path bifurcation has been observed in previous direct-MD simulations for a few reactions in the literature.^{9,10} Most of them are related to a symmetrical PES, in which a minimum energy path (MEP) from the TS that separates the reactant and product regions leads through a valley-ridge inflection (VRI) point to another TS separating two symmetrical products.²¹ Trajectories starting from the first TS proceed toward the second TS and bifurcate before reaching the second TS to give two products in statistically equal amounts. When a small perturbation, such as an isotope or a remote substituent, is introduced, the two products would be formed in different amounts.⁹ The product ratio is controlled by the way trajectories adopt the course on the way from the first TS to the second TS. Path bifurcation may occur on a different type of PES, in which MEP from a TS leads to one product that is separated by the second TS from another product located nearby on the PES.¹⁰ Bifurcation on such an asymmetrical PES may occur when trajectories move off the MEP dynamically and get over a barrier toward the second product region.

The present Beckmann rearrangement/fragmentation falls in the second category. In this case, trajectories from the TSs for **8-X** ($X = p\text{-NH}_2, p\text{-MeO}$) led to the fragmentation product region, whereas those for **8-X** ($X = p\text{-NO}_2, p\text{-CN}$) went mostly to the rearrangement product region. In these cases, the trajectories basically followed the IRCs. For other borderline substrates, however, trajectories starting from the respective TS bifurcated and led to two product regions, despite that IRCs lead either of the two regions. It is important to point out that more F-type trajectories were detected for **8-X** with a more electron-donating substituent.

These observations are explained by the existence of the barrier separating the two product regions and the shift of the barrier with substituent. Two-dimensional PESs near the product regions of **8-H** and **8-p-CN** are illustrated in Fig. 6, in which the abscissa is the $\text{CH}_2\text{--N--CH}_2\text{Ar}$ angle and the ordinate is the $\text{N--CH}_2\text{Ar}$ distance.

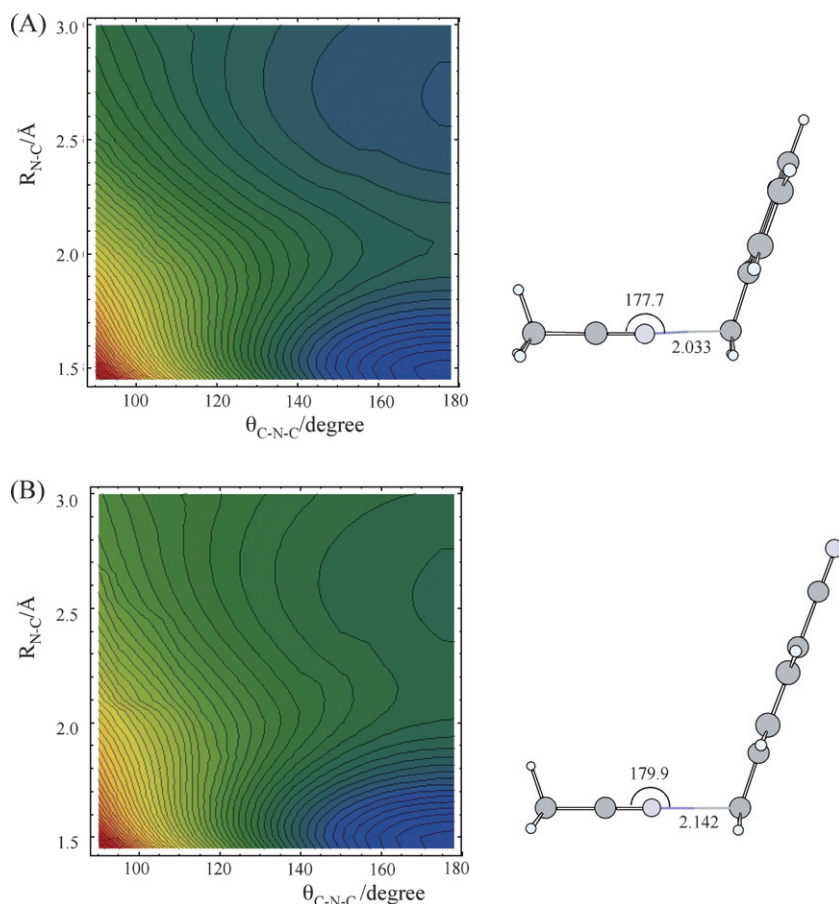


Fig. 6 Two-dimensional PESs and the TS structures between the two product regions for (A) **8-H** and (B) **8-p-CN**. The abscissa is the angle C–N–CH₂Ar in degrees and the ordinate is the atomic distance CN–CH₂Ar in Å.

The leaving group is not included in the PES calculations, since the inclusion of H₂O requires impractical three-dimensional treatments. Thus, the PESs in Fig. 6 are not the exact surfaces of the reactions, but they are nevertheless useful to examine the shape of the surfaces qualitatively, especially near the product regions where the leaving group is nearly cleaved. The PES and the structures of the TSs separating the two product regions in Fig. 6 illustrate that the barrier exists between the two product regions and that its location shifts with the substituent. Reaction trajectories coming down from the left toward the right of the map would reach either the fragmentation or rearrangement product region depending on the location of the barrier.

The MD trajectories follow the same courses as IRCs when the initial kinetic energy is small. By contrast, when enough kinetic energy is provided, simulations for the borderline substrates give both type R and F trajectories, due to wider variations of the trajectories. In such cases, more F type trajectories would be observed for **8-X** with a more electron-donating substituent, since the barrier shifts toward a less stable side of the products. Thus, since an electron-donating substituent makes the fragmentation product more stable, the barrier moves toward the rearrangement side, and then more trajectories go to the fragmentation side. The shift of the barrier

seen in Fig. 6 is consistent with the Leffler–Hammond principle¹⁸ and agrees with the prediction by the Thornton rule.²²

3 Concluding remarks

The MO calculations indicated that the reaction of **8-X** goes through a single TS either for the rearrangement or fragmentation routes, and the rearrangement/fragmentation product switching occurs as a function of the substituent. The introduction of an electron-donating substituent into the phenyl ring changes the mechanism from the rearrangement for $X = p\text{-NO}_2$, $p\text{-CN}$, $p\text{-CHO}$, H , $m\text{-Me}$, $m,m'\text{-Me}_2$, and $p\text{-Me}_2$ to fragmentation for $X = p\text{-MeO}$ and $p\text{-NH}_2$ (at MP2). On the other hand, the overall reactivity increases with a more electron-donating substituent on the phenyl ring in such a manner that the relative reactivity follows nicely the Hammett equation, and the structure of the TS varies with X in a manner consistent with the Hammond postulate in spite of the mechanistic changes with substituent. It is implied that Hammett plots and analyses of TS structures may give incorrect information of the reaction mechanism.

Trajectory calculations revealed that two products are formed through a single TS for borderline substrates. It is concluded that a conventional reactivity-selectivity argument and mechanistic assignment based on the TS theory may not always be applicable even to a well-known textbook organic reaction.

It should also be noted that the dynamically determined product ratio is governed by the electronic nature of substituents in a manner consistent with traditional electronic theory. Thus, the computationally detected substituent effects on the product distribution are readily reconciled with traditional reaction theory, which means that such a path bifurcation phenomenon would not easily be detected by experiment, unless critical examinations of experimental results were made. Measurements of substituent effects and KIEs, which are common means to detect variation of TS structures and reaction mechanisms, should be planned with care, since these experimental methods applied to rate processes do not afford information of possible path bifurcation occurring after the TS.

Nevertheless, careful kinetic and product analyses may allow us to detect path bifurcation experimentally. When two products are formed *via* parallel reactions, the overall rate can be divided into individual reactions on the basis of the product ratio, and substituent effects for each reaction thus obtained should give a linear Hammett plot. If, on the other hand, two products are formed through path bifurcation after the rate-determining TS, the TS has little relevance to the product-determining mechanism, and therefore the above-mentioned method of dividing the overall rate into two individual rates is likely to fail. Thus, careful examination of the correlation between rates and product ratios for a series of substrates may allow detection of path bifurcation.

Although extensive kinetic and product analysis experiments are required to prove the path bifurcation, the present experimental results, though preliminary, appear to cast doubt in interpreting the results in terms of two concurrent reaction pathways as commonly assumed, and provide support for dynamics effect and the bifurcation for the Beckmann reaction.

4 Experimental methods

All substituted oximes were synthesized from corresponding benzaldehydes by nitroaldol with EtNO_2 ,²³ Fe reduction,²⁴ and oximation with NH_2OH . The sulfonate esters, **2-X** and **3-X** ($X = p\text{-CH}_3$, H , $p\text{-Cl}$, $m\text{-Cl}$, and $p\text{-CF}_3$) were prepared by Tipson's method from the corresponding oximes and 2-naphthalenesulfonyl chloride in pyridine.²⁵ The authentic samples of the reaction products (**4-X**, **5-X**, **6-X**, **7-X**) were either isolated from the reaction mixture or synthesized separately.

The reaction rates were measured by running the reactions in 80% aq. MeCN for **2-X** and 90% aq. MeCN for **3-X** at 25.0 ± 0.1 °C in the presence of 1.1 equiv. of *N,N*-dimethylaniline. All reactions proceeded quantitatively, and the rates were determined photometrically by following the decrease of the absorbances of the sulfonates at their absorption maxima at 325–326 nm. Material balance and product distribution were measured by analyzing the reaction mixture after 10 half-lives by means of GC and HPLC. The sensitivities of the products in the GC and HPLC measurements were calibrated by using authentic samples, which gave the material balances of $101 \pm 4\%$.

Computational methods

Reactants (**8-X**), **Int**, TSs, and products ($\text{XC}_6\text{H}_4\text{CH}_2^+$, CH_3CN , and $\text{CH}_3\text{C}^+=\text{NCH}_2\text{C}_6\text{H}_4\text{X}$) were fully optimized both at HF/6-31G* and MP2/6-31G* with Gaussian 03.²⁶ Full frequency calculations were carried out for all optimized structures to confirm whether the structures are on a minimum or a saddle point on the PES. IRC calculations were performed for all TSs at both computational levels.

Trajectory calculations were carried out by using three different methods, HONDO,²⁷ PEACH,²⁸ and G03.²⁶ The kinetic temperature was in most cases 50 K, and some calculations with 10 K kinetic temperature were carried out for comparison. Simulations with HONDO were initiated at each TS for a series of substituted derivatives with initial atomic velocities assigned from a random Maxwell–Boltzmann distribution with the total kinetic energy consistent with the simulation temperatures and run with a step size of 0.5 fs.⁷ The method did not adopt the quasiclassical simulation methodology that assigns zero-point vibrational energies to the harmonic modes of vibrations as initial conditions, in order to minimize a side effect from unrealistic zero-point energy flow from transverse vibrational modes into the reaction coordinate mode. A velocity rescaling algorithm similar in form to the constant temperature algorithm of Berendsen *et al.*²⁹ was used with a relaxation time $t = 2000$ fs to mimic a slow energy transfer between the solute and an imaginary solvent bath. Calculations with PEACH were carried out in the same manner as HONDO, except that total energy was preserved during the simulations. G03 trajectory calculations were performed for the TS of each substituted substrate with BOMD keyword, which adopts the Hessian-based predictor-corrector method and quasiclassical sampling.

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