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## A Precise Measurement of the Muon Neutrino–Nucleon Inclusive Charged Current Cross Section off an Isoscalar Target in the Energy Range $2.5 < E_\nu < 40 \text{ GeV}$ by *NOMAD*

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# A precise measurement of the muon neutrino–nucleon inclusive charged current cross section off an isoscalar target in the energy range $2.5 < E_\nu < 40$ GeV by NOMAD

NOMAD Collaboration

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## Abstract

We present a measurement of the muon neutrino–nucleon inclusive charged current cross section, off an isoscalar target, in the neutrino energy range  $2.5 \leq E_\nu \leq 40$  GeV. The significance of this measurement is its precision,  $\pm 4\%$  in  $2.5 \leq E_\nu \leq 10$  GeV, and  $\pm 2.6\%$  in  $10 \leq E_\nu \leq 40$  GeV regions, where significant uncertainties in previous experiments still exist, and its importance to the current and proposed long baseline neutrino oscillation experiments.

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## 1. Motivation

The muon neutrino–nucleon inclusive charged current ( $\nu_\mu$ -N CC) cross section has been well measured at high neutrino energies ( $30 \leq E_\nu \leq 250$  GeV), primarily by the CCFR [1] and the CDHSW [2] experiments. The average absolute  $\nu_\mu$ -N CC cross section, where ‘N’ is a nucleon in an isoscalar target, above  $E_\nu$  of 30 GeV,  $\sigma^{\text{CC}}(\nu_\mu N) = (0.677 \pm 0.014) \times 10^{-38}$  cm<sup>2</sup>/GeV, is measured to a 2.1% precision. In contrast the  $\sigma^{\text{CC}}(\nu_\mu N)$  is imprecisely measured below 30 GeV. Previous measurements are summarized in [3]. Accurate determination of  $\sigma^{\text{CC}}(\nu_\mu N)$  below  $E_\nu$  of 30 GeV is of interest in its own right, and offers insight into lower energy CC processes such as quasi-elastic and resonance interactions, and their transition into the deep inelastic scattering region. The current and the proposed long baseline neutrino experiments, such as MINOS [4] and NOvA [5] at Fermilab and T2K in Japan [6], address the atmospheric  $\nu$  oscillations at the mass-difference,  $\Delta m_{23}^2 \approx 2.5 \times 10^{-3}$  eV<sup>2</sup>. Given their typical flight path of a few hundred kilometers, they use neutrino beams with energies well below 30 GeV. Cross sections in this region should be precisely known to accurately interpret the results of these

experiments. The NOMAD data are suitable for such a precision  $\sigma^{\text{CC}}(\nu_\mu N)$  measurement due to the large  $\nu$ -interaction sample, good low-energy resolution and a  $\nu_\mu$  flux which spans  $\mathcal{O}(1) \leq E_\nu \leq 300$  GeV with a mean energy of 24.3 GeV.

## 2. The beam and the detector

The neutrino oscillation magnetic detector (NOMAD) experiment at CERN used a neutrino beam produced by the 450 GeV SPS-protons striking a beryllium target and producing secondary  $\pi^\pm$ ,  $K^\pm$ , and  $K_L^0$  mesons. The positively charged mesons were focussed by a system of collimators, a magnetic horn and a reflector into a 290 m long evacuated decay pipe. Decays of  $\pi^\pm$ ,  $K^\pm$ , and  $K_L^0$  produced the SPS neutrino beam. The average flight path of the neutrinos to NOMAD was 628 m; the detector being 836 m downstream of the Be-target. The SPS beamline and the neutrino flux incident at NOMAD are described in [7] and [8].

NOMAD was designed to search for  $\nu_\mu \rightarrow \nu_\tau$  oscillations at  $\Delta m^2 \geq 5$  eV<sup>2</sup>, and in this  $\Delta m^2$  range it set the current best limit on this search [9]. The experiment ran from 1995 to 1998, with a cumulative  $55 \times 10^{18}$  SPS protons on the Be target, and recorded over 1.7 million neutrino interactions in its active drift-chamber (DC) target. These data are unique in that they constitute the largest high resolution neutrino data sample with accurate identification of  $\nu_\mu$ ,  $\bar{\nu}_\mu$ ,  $\nu_e$ , and  $\bar{\nu}_e$  in the energy range  $\mathcal{O}(1) \leq E_\nu \leq 300$  GeV. In addition, upstream of the active-DC target, the experiment recorded over 2 million  $\nu$ -interactions in

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the Al-coil, and over 20 million in the Fe-scintillator calorimeter (FCAL).

The NOMAD apparatus, described in [10], was composed of several sub-detectors. The active target comprised 132 planes of  $3 \times 3 \text{ m}^2$  drift chambers with an average density similar to that of liquid hydrogen ( $0.1 \text{ gm/cm}^3$ ) [11]. On average, the equivalent material in the DC encountered by particles produced in a  $\nu$ -interaction was about  $0.5 X_0$  and a quarter of an interaction length ( $\lambda$ ). The fiducial mass of the NOMAD DC-target, composed primarily of carbon (64%), oxygen (22%), nitrogen (6%), and hydrogen (5%), was 2.7 tons. The measured composition of the target was 52.43% protons and 47.57% neutrons. The correction for non-isoscalarity was about 5%. Downstream of the DC, there were nine modules of transition radiation detectors (TRD), followed by a preshower (PRS) and a lead-glass electromagnetic calorimeter (ECAL). The ensemble of DC, TRD, and PRS/ECAL was placed within a dipole magnet providing a 0.4 T magnetic field. Outside the magnet was a hadron calorimeter (HCAL), followed by two muon-stations comprising large area drift chambers separated by an iron filter. The two muon-stations, placed at 8- and 13- $\lambda$  downstream of the ECAL, provided a clean identification of the muons.

The charged tracks in the DC were measured with an approximate momentum ( $p$ ) resolution of  $\sigma_p/p = 0.05/\sqrt{L} + 0.008p/\sqrt{L^5}$ ,  $p$  in GeV and  $L$  in meters, and uniquely offered charge separation in the energy range of interest. The  $\pi^0$  component of the  $\nu$ -hadronic jet was measured by the ECAL with a resolution of  $\sigma_E/E = 3.2\%/\sqrt{E} + 1\%$ . The detailed individual reconstruction of each charged and neutral track and their precise momentum vector measurement enabled a quantitative description of the event kinematics: the strength and basis of NOMAD analyses. In a  $\nu_\mu$ -CC interaction, in addition to the three traditional variables, energy ( $E_\mu$ ), angle ( $\theta_\mu$ ) of the emergent muon, and the hadron energy ( $E_{\text{HAD}}$ ), the detector uniquely offered a measurement of the missing transverse momentum ( $p_T$ ) vector in a plane transverse to the neutrino direction.

### 3. The analysis

The  $\sigma^{\text{CC}}(\nu_\mu N)$  was measured by dividing the fully corrected  $\nu_\mu$ -CC data by the corresponding  $\nu_\mu$ -flux as a function of  $E_\nu$ . We first describe the measurement of the numerator. In a  $\nu_\mu$ -CC interaction, the neutrino energy ( $E_\nu$ ) was measured by adding the energies of the muon ( $E_\mu$ ) and particles composing the hadron-jet ( $E_{\text{HAD}}$ ) yielding the total visible energy ( $E_{\text{VIS}}$ ) of the interaction. The observed CC-data, binned in  $E_\nu$  commensurate with resolution and statistics, were corrected for the detector acceptance, the efficiency of the cross-section selection cuts, and the reconstruction smearing effects using  $\nu_\mu$ -CC Monte Carlo (MC) samples.

To produce a clean sample of  $\nu_\mu$ -CC events, the following selection criteria were imposed. First, the event must have at least one negative track ( $\mu^-$ ) and the vertex position be within the fiducial volume. Since the  $\sigma^{\text{CC}}(\nu_\mu N)$  analysis was entirely dominated by systematic errors, more stringent fiducial cuts

were imposed than those used in statistical-error limited analyses such as [9]. The momentum vector of the muon, and other charged particles, were measured in the B-field of the detector by the DC. The muon chambers were used only to identify muons that succeeded in penetrating the ECAL, HCAL and additional steel. Accordingly, the requirement of a successful match between a drift chamber track to track-segments in both muon chambers yielded the muon identification ( $\mu$ -ID). The  $P_\mu > 2.5 \text{ GeV}$  cut, dictated by the muon energy loss in penetrating the thickness of the HCAL preceding the first muon station, defined the low energy limit of our measurement. The polar angle of the muon with respect to the incident neutrino direction,  $\theta_\mu$ , was required to be less than 0.5 radians. Finally, for the 1-track sample a cut on the transverse muon-momentum,  $p_T^2 = (P_\mu \times \theta_\mu)^2 > 0.0025 \text{ GeV}^2$ , was used to eliminate the inverse muon decay ( $\nu_\mu + e^- \rightarrow \mu^- + \nu_e$ ) events with minimal loss of efficiency.

The standard NOMAD  $\nu$ -event generator, NEGLIB, and the detailed Monte Carlo simulation was based upon LEPTO 6.1 [12] and JETSET [13] generators for neutrino interactions and on a GEANT [14] based program for the detector response. The parton content of the nucleon were taken from Ref. [15]. The  $\nu_\mu$ -MC included deep-inelastic scattering (DIS), resonance (RES), and quasi-elastic (QE) processes. The relative abundance of DIS:RES:QE samples, averaged over the  $\nu_\mu$ -flux, was taken to be 1.0:0.031:0.024. The (QE + RES) to DIS, and QE to RES, cross sections were separately varied by  $\pm 15\%$  and the resulting small difference in  $\sigma^{\text{CC}}(\nu_\mu N)$  was taken as a systematic error. The acceptance computed using the total number of generated MC in the standard NOMAD fiducial volume [9] and the corresponding number of reconstructed MC events passing event selection cuts took into account the bias in the true average energy due to the event reconstruction and selection process. It should be noted that the standard NOMAD fiducial volume used for generated MC (the denominator in acceptance calculation) was about 22% larger than that used for the reconstructed sample. A small impurity (0.7%) due to neutral-current (NC), from  $\nu$  and  $\bar{\nu}$  interactions, induced  $\mu^-$ -sample was corrected using the NC-MC estimation. The effects of the selection cuts on data and Monte Carlo are summarized in Table 1.

### 4. The $\nu_\mu$ -flux and the absolute normalization

Cross-section measurements require a knowledge of the  $\nu$ -flux. Neutrinos in the SPS beam were mainly from  $\pi$ ,  $K$ , and  $\mu$  decays. The uncertainty in modeling these secondary particles, and hence the  $\nu$ -flux, was—and for all the  $\sigma^{\text{CC}}(\nu_\mu N)$  measurements has been—the dominant source of systematic error. A dedicated measurement of  $\pi/K$  yields in 450 GeV  $p$ -Be collision at various secondary energies and angles was undertaken by the SPY experiment [16]. The SPY measurement of the  $\pi^\pm/K^\pm$  yields was carried out at discrete energies spanning 7 to 135 GeV, and a detailed transverse-momentum ( $P_T$ ) scan at 15 and 40 GeV that were especially useful to the present measurement. A previous measurement of  $\pi/K$  yield in a 400 GeV  $p$ -Be collision by Atherton et al. [17] was also used in the  $\nu$ -flux determination. Other systematic uncertainties in the  $\nu_\mu$ -

Table 1  
Selection criteria for  $\nu_\mu$  charged current events: The numbers of data, and normalized MC samples from  $\nu_\mu$ -CC, NC, and  $\nu_e$ -,  $\bar{\nu}_e$ -, and  $\bar{\nu}_\mu$ -CC events passing the  $\sigma^{\text{CC}}(\nu_\mu N)$  analysis cuts are shown

Cut	Data	QE	RES	DIS	$\nu_\mu$ -CC	NC	$\nu_e$	$\bar{\nu}_e$	$\bar{\nu}_\mu$
Generated in fid		32198.8	42869.7	1364812.4	1439880.9	547103.1	21598.3	2159.9	35996.0
Reconstructed	4022549.0	27985.2	37120.5	1182505.1	1247610.9	394053.7	18905.1	1881.3	31033.7
Fiducial volume	1815455.0	20265.1	31040.1	1122888.6	1174193.9	313487.8	18131.8	1547.6	27201.8
Negative muon	1069609.0	20114.0	30816.5	987008.8	1037939.3	6707.8	325.5	24.1	279.4
Quality cuts	1043691.0	19960.3	30527.3	985255.8	1035743.3	6698.7	325.5	24.1	279.3
$E_\mu > 2.5$	1038783.0	19941.9	30509.7	980265.8	1030717.4	6484.5	316.0	23.2	270.0
$\theta_\mu < 0.5$ rad	1035260.0	19939.4	30503.0	978387.4	1028829.8	6476.8	314.8	23.1	267.9
$p_T^2 > 0.0025$	1035107.0	19906.7	30472.9	978383.2	1028762.8	6476.8	314.8	23.1	267.9

flux determination arose from the variation in the position of the primary proton beam and the simulation of the propagation of secondaries through the beam line. The energy dependent relative  $\nu_\mu$  flux errors [8] were the largest source of systematic error in this analysis.

In this analysis only the relative  $\nu_\mu$ -flux, i.e., number of  $\nu_\mu$  in  $E_\nu$  bins, obtained using the SPY/Atherton measurements, was used. The absolute normalization of the  $\nu_\mu$ -flux was fixed using the world average of  $\frac{\sigma(\nu N)}{E}$  above 40 GeV. The absolute flux normalization was computed in the following energy regions: 40–100 GeV, 40–150 GeV, 50–150 GeV, and 50–200 GeV. Variations in the normalization, from these control regions, bracketed the error in the absolute flux normalization process. In addition, the 2.1% error in world average cross section was included into our error calculation.

## 5. Systematic uncertainties

In what follows, we enumerate sources of systematic errors affecting the numerator. The muon identification-efficiency and energy-scale were the two most important measurables in the  $\sigma^{\text{CC}}(\nu_\mu N)$  analysis. First, a precise understanding of the muon-chamber efficiency and stability was crucial. In a dedicated run in 1996 during the gap between the two neutrino spills from the SPS, we accumulated a large statistics of muons. This ‘flat-top  $\mu$ ’ sample was identified by the veto-counter and the most upstream DCs. The energy spectrum of the flat-top muon sample, spanning 4 to 50 GeV with a mean energy of 16 GeV, was similar to that induced by the  $\nu_\mu$ -CC events. The measured absolute efficiency of the  $\mu$ -ID for this sample was 99.96%, in agreement with a detailed Monte Carlo simulation of the flat-top muons. Next, we studied the stability of the  $\mu$ -identification by using the fraction of events with an identified muon,  $[\rho(\mu\text{-ID})]$ , as a function of time spanning 1995 through 1998, and as a function of 15 sections of the muon chambers. The  $\rho(\mu\text{-ID})$  was stable to better than 1% over this four-year period. The distribution of  $\rho(\mu\text{-ID})$ , measured over 47 running periods, was consistent with a Gaussian distribution with an error in the mean of 0.15%. These consistency between data and MC simulation of  $\mu$ -identification ensured the accuracy of the  $\nu_\mu$ -CC efficiency computed by the Monte Carlo. The systematic errors due to the small difference in the absolute  $\mu$ -ID efficiency between data and MC and the variation in  $\rho(\mu\text{-ID})$  were included in the analysis.

In NOMAD, the  $E_\mu$ -scale was determined by the accurately measured B-field and a precise DC-alignment accomplished by using several million beam muons traversing the detector throughout the neutrino runs. The momentum scale was checked by using the invariant mass ( $M_{K_S}$ ) of over 30000 reconstructed  $K_S^0$  in the CC and NC data. The systematic error on the  $E_\mu$ -scale was determined to be 0.2%.

Neutrino-induced hadron jets, including charged and neutral particle multiplicity and fragmentation, are poorly understood resulting in a discrepancy between the hadronic energy of data and MC. We reduced this discrepancy by correcting the simulated hadronic energy  $E_{\text{HAD}}$  by a constant factor  $\kappa_H$ , based on the distribution of  $y_{Bj} = E_{\text{HAD}}/E_\nu = E_{\text{HAD}}/(E_{\text{HAD}} + E_\mu)$  in Monte Carlo and data. We relied on the precise measurement of  $E_\mu$ . To determine the  $\kappa_H$  trials were made to minimize the  $\chi^2$  between data and MC  $y_{Bj}$ - and  $E_{\text{HAD}}$ -distributions, for events with  $E_{\text{HAD}} \geq 2.5$  GeV, by varying  $\kappa_H$  from 0.9 to 1.1 in steps of 0.002 in the MC. The  $\chi^2$  was minimized at  $\kappa_H$  of 0.950, i.e., the MC overestimated  $E_{\text{HAD}}$  by 5%. The comparison of the  $y_{Bj}$  distribution between data and the uncorrected-MC is shown in Fig. 1(a), where  $\frac{\chi^2}{\text{DoF}}$  is 795.1/49. The corresponding comparison after correcting the MC- $E_{\text{HAD}}$  is shown in Fig. 1(b), where  $\frac{\chi^2}{\text{DoF}}$  is 89.6/49. To determine the error on  $\kappa_H$  we formed a ‘scaled’- $\chi^2$  which yielded the scaled- $\frac{\chi^2}{\text{DoF}}$  equal to unity at  $\kappa_H$  of 0.950. This was achieved by increasing the errors by 40%. Fig. 1(c) shows the scaled- $\chi^2$  as a function of  $\kappa_H$ . An increase of 1.0 from the minimum in the scaled- $\chi^2$  (see the inset) was used to set the uncertainty on the optimum  $\kappa_H$  value of 0.950. Additionally, the fiducial and kinematic cuts were varied and the range in  $\kappa_H$  was redetermined for unity variation in the scaled- $\chi^2$ . We concluded that an error of  $\pm 0.006$  bracketed the error on  $\kappa_H$ . Since  $\kappa_H$  was determined over the entire range of  $E_\nu$ , to cover possible variations in  $\kappa_H$  as a function of  $E_\nu$ , we increased the scale-error by 50%. Correcting  $E_{\text{HAD}}$  in the MC by  $\kappa_H$  also improved the agreement between the data and MC distributions of other kinematic variables:  $Q^2$ ,  $W^2$ , and  $x_{Bj}$  where the improvement was comparable to that shown in Fig. 1(b). The  $E_{\text{HAD}}$  correction factor determined in this analysis is closer to unity than the value of 0.93 used in our previous analyses [18] because of better tuning of the Monte Carlo and a reprocessing of the data that improved the reconstruction of high multiplicity events. The difference in the  $\sigma^{\text{CC}}(\nu_\mu N)$  due to the  $\pm 0.009$  uncertainty on  $\kappa_H$  was computed and assigned

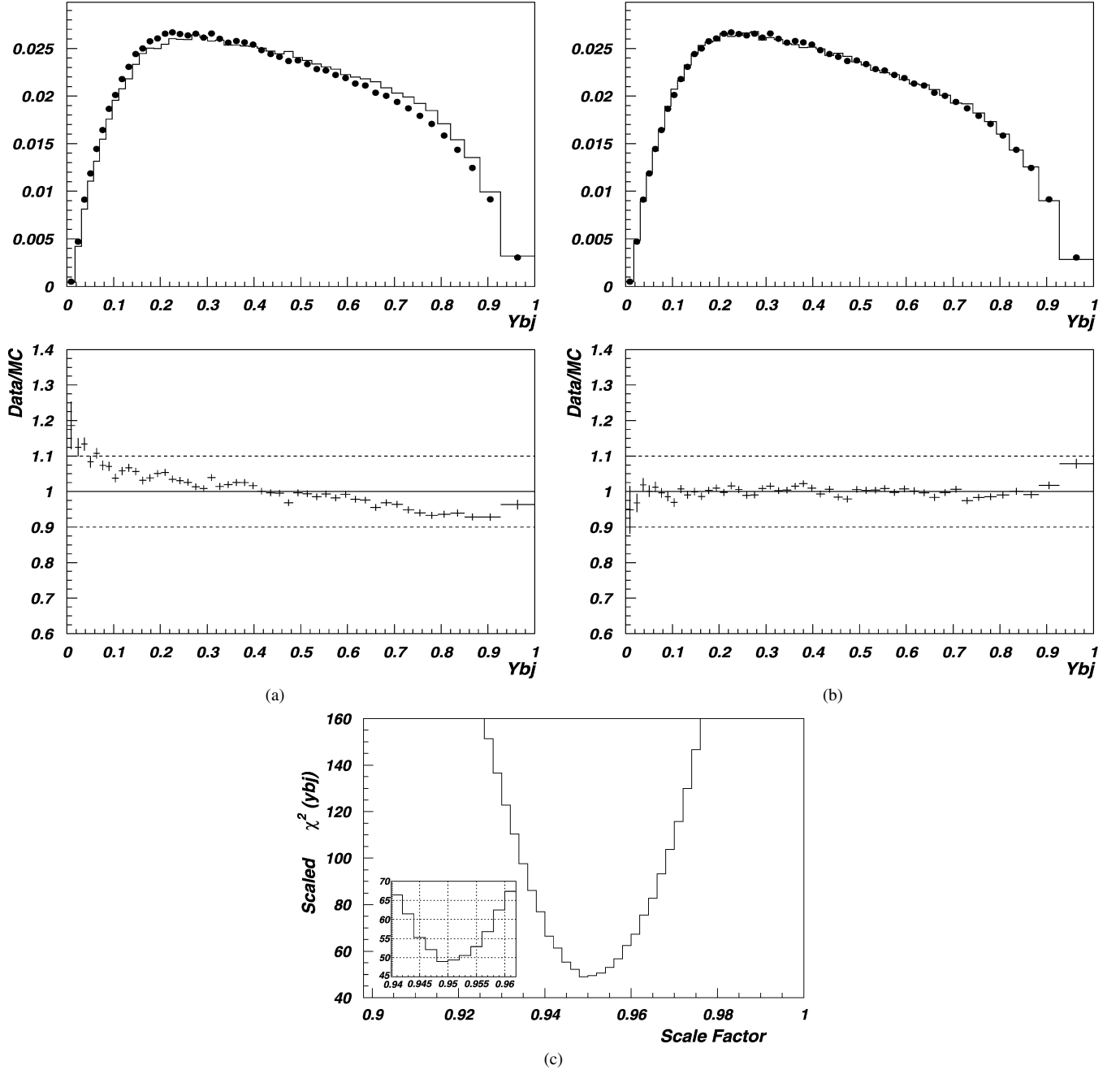


Fig. 1. The data and MC  $y_{Bj}$ -distributions: The  $y_{Bj}$  distributions for data (symbols) and MC (histogram) (a) before and (b) after rescaling  $E_{HAD}$  are shown in the top; the ratio of data to Monte Carlo for the two distributions are also shown. The lower plot (c) shows the scaled- $\chi^2$  distribution for  $y_{Bj}$  as a function of  $E_{HAD}$ -scale.

as the systematic error. This systematic uncertainty would have to be a factor of 2.5 times larger to make it one of the dominant systematic errors in the analysis. Although the 0.9% error in the  $E_{HAD}$ -scale is adequate for the present inclusive  $\sigma^{CC}(\nu_\mu N)$  measurement, efforts are underway to reduce this error to the 0.5% level using improved modeling [19] and analysis for the future  $\nu_\mu$ -CC differential cross section as a function of  $E_\nu$ ,  $x_{Bj}$ , and  $y_{Bj}$ , and the weak mixing angle measurements. Table 2 lists the systematic errors on the  $\sigma^{CC}(\nu_\mu N)/E_\nu$  as a function of visible energy.

Radiative corrections [20] that affected measurables, such as  $E_\mu$ ,  $\theta_\mu$ , and  $E_{HAD}$ , were folded into the  $\sigma^{CC}(\nu_\mu N)$  mea-

surement as a function of  $E_\nu$ . The dominant radiative effect, typically less than 1% on  $\sigma/E_\nu$ , occurred when a photon, radiated by the muon, was measured as part of the hadronic system. No other effort was made to correct the  $\nu_\mu$ -CC cross section to the Born-level.

## 6. Result

After the  $E_{HAD}$ -scale correction, we present the  $E_{VIS}$  comparison between data and MC in Fig. 2. Except for the lowest energy bin, the agreement is better than 2% in the energy range shown. We point out that the  $\nu_\mu$ -CC cross section was

Table 2  
Systematic uncertainties on  $\sigma/E$  in neutrino energy range

$E_{\text{VIS}}$ (GeV)	Relative flux	Normalization region	$\mu$ -acceptance	$E_{\text{HAD}}$ -scale	QE:RES:DIS
2.5–10	0.026	0.005	0.004	0.008	0.002
10–15	0.018	0.004	0.001	0.004	0.001
15–30	0.016	0.005	0.001	0.006	0.000
30–50	0.022	0.005	0.000	0.003	0.000
50–100	0.040	0.004	0.000	0.005	0.000
100–300	0.051	0.004	0.002	0.010	0.000

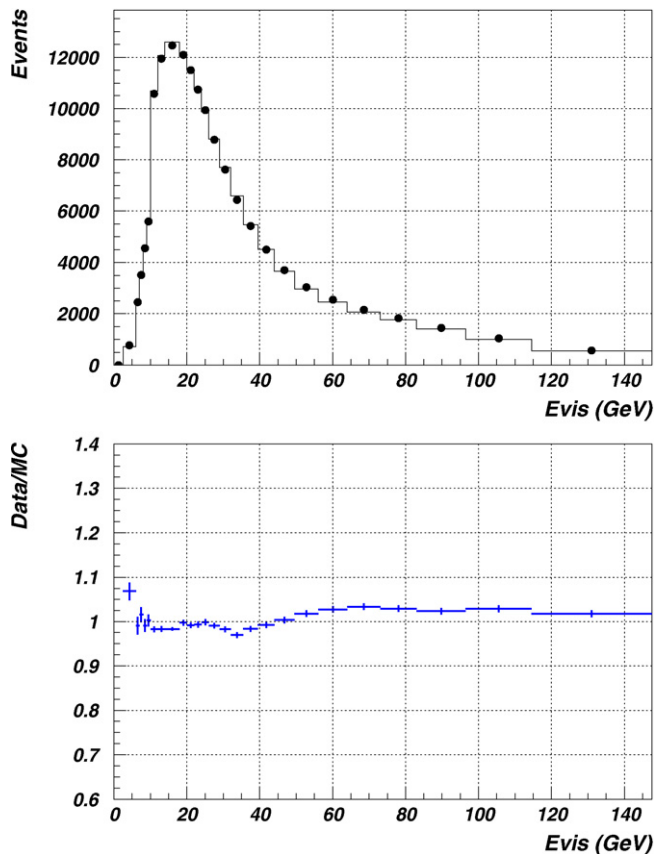


Fig. 2. Distributions of  $E_{\text{VIS}}$  for data (symbols) and Monte Carlo (histogram): The  $E_{\text{HAD}}$  correction is applied to the MC. Only the statistical errors are shown. The ratio of data to Monte Carlo is also presented.

not modified in the Monte Carlo. The inclusive  $\nu_{\mu}$ -CC cross-sections were derived from this distribution. The final result of the measurement of the inclusive  $\nu_{\mu}$  charged current (CC) cross section is summarized in Table 3. The  $E_{\nu}$ -range, the average- $E_{\nu}$ , number of observed data and background (mainly from NC) events passing the selection criteria are listed respectively in the first four columns. The observed data are corrected by subtracting the background, and then dividing by the efficiency (5-column). The cross section, after correcting for non-isoscalarity, was calculated by dividing the corrected data (6-column) by the flux after absolute normalization (7-column) and the average- $E_{\nu}$ . The  $\sigma^{\text{CC}}(\nu_{\mu}N)/E_{\nu}$  with the statistical, systematic, and total errors are shown in the last four columns of Table 3.

The inclusive  $\nu_{\mu}$  CC cross section divided by  $E_{\nu}$  is plotted as a function of  $E_{\nu}$  in Fig. 3 together with existing

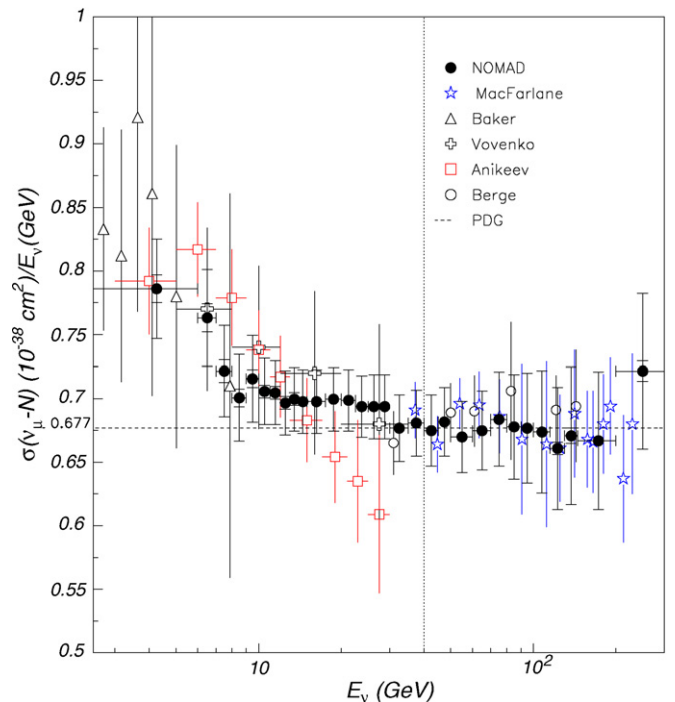


Fig. 3. Inclusive  $\nu_{\mu}$ -N charge current cross section vs.  $E_{\nu}$ : The  $\sigma^{\text{CC}}(\nu_{\mu}N)/E_{\nu}$  is plotted as a function of  $E_{\nu}$ , where  $N$  represents an isoscalar nucleon within the NOMAD target. The outer (inner) error bars show the total (statistical) error. Other measurements in this plot are by D.B. MacFarlane et al. [1], J.P. Berge et al. [2], N.J. Baker et al. [21], A.S. Vovenko et al. [22], and V. Anikeev et al. [23]. The region  $E_{\nu} \geq 40$  GeV was used to normalize the  $\sigma^{\text{CC}}(\nu_{\mu}N)/E_{\nu}$  to the asymptotic world average [3], shown as the dashed line, derived from high energy data.

measurements. From this plot, agreement with the existing data above  $E_{\nu} \geq 30$  GeV is seen:  $\sigma^{\text{CC}}(\nu_{\mu}N)/E_{\nu}$  is flat above 30 GeV; it rises at lower energies due to the increasing presence of the non-scaling processes. In the sub 30 GeV region, the NOMAD measurements improve the precision.

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Table 3

Summary of the  $\nu_{\mu}$ -CC cross section,  $\sigma(10^{-38} \text{ cm}^2)/E$  (GeV), analysis: The fifth-column represents the efficiency folded with the acceptance, see Section 3. The  $\sigma/E_{\nu}$  is presented for an isoscalar nucleon within the NOMAD target

$E_{\nu}$ -range (GeV)	Avg. $E_{\nu}$ (GeV)	Data	Bkgd	Eff.	Cor. Data	Flux ( $10^5$ )	$\sigma/E_{\nu}$	Stat Err.	Syst. Err.	Total Err.
2.5–6.0	4.60	5429.0	51.2	0.409	13296.9	4.07	0.786	0.011	0.035	0.037
6.0–7.0	6.50	4917.0	45.0	0.452	10778.5	2.40	0.763	0.011	0.036	0.038
7.0–8.0	7.50	7011.0	53.2	0.445	15625.2	3.20	0.722	0.009	0.035	0.036
8.0–9.0	8.50	9119.0	46.0	0.445	20369.0	3.79	0.701	0.007	0.033	0.034
9.0–10.0	9.50	11192.0	50.5	0.443	25171.9	4.10	0.716	0.007	0.033	0.034
10.0–11.0	10.50	20244.0	87.9	0.704	28629.3	4.29	0.706	0.005	0.026	0.026
11.0–12.0	11.50	22051.0	91.2	0.698	31471.8	4.31	0.705	0.005	0.024	0.025
12.0–13.0	12.50	23349.0	100.7	0.685	33936.8	4.33	0.697	0.005	0.024	0.025
13.0–14.0	13.50	24433.0	94.3	0.686	35462.1	4.17	0.700	0.005	0.024	0.025
14.0–15.0	14.50	24802.0	91.1	0.682	36249.3	3.98	0.698	0.004	0.025	0.025
15.0–17.5	16.20	62447.0	249.7	0.678	91750.9	9.00	0.698	0.003	0.025	0.025
17.5–20.0	18.70	60825.0	246.5	0.686	88315.5	7.48	0.700	0.003	0.025	0.025
20.0–22.5	21.20	57249.0	240.2	0.690	82590.0	6.18	0.699	0.003	0.024	0.024
22.5–25.0	23.70	51919.0	226.6	0.691	74772.6	5.04	0.694	0.003	0.024	0.024
25.0–27.5	26.20	46696.0	233.4	0.693	67054.3	4.09	0.694	0.003	0.025	0.025
27.5–30.0	28.70	41462.0	239.3	0.696	59235.3	3.30	0.694	0.003	0.025	0.025
30.0–35.0	32.30	68858.0	431.4	0.708	94730.8	4.91	0.677	0.003	0.026	0.026
35.0–40.0	37.30	54059.0	420.5	0.704	75291.1	3.33	0.681	0.003	0.026	0.026
40.0–45.0	42.40	43650.0	379.9	0.715	61212.5	2.35	0.675	0.003	0.028	0.028
45.0–50.0	47.40	36135.0	326.3	0.718	49084.9	1.71	0.682	0.004	0.027	0.027
50.0–60.0	54.60	57357.0	618.2	0.733	77653.8	2.35	0.670	0.003	0.028	0.028
60.0–70.0	64.70	45880.0	509.8	0.733	61753.1	1.57	0.675	0.003	0.031	0.031
70.0–80.0	74.80	38523.0	409.6	0.700	54226.5	1.18	0.684	0.003	0.037	0.037
80.0–90.0	84.80	32054.0	309.1	0.666	47043.6	0.92	0.678	0.004	0.041	0.041
90.0–100.0	94.80	25884.0	231.8	0.636	39517.5	0.70	0.677	0.004	0.043	0.043
100.0–115.0	107.00	29673.0	258.4	0.628	46821.5	0.72	0.674	0.004	0.048	0.048
115.0–130.0	122.00	20327.0	176.7	0.608	32923.4	0.46	0.661	0.005	0.048	0.048
130.0–145.0	136.90	14204.0	117.7	0.583	24337.2	0.29	0.671	0.006	0.054	0.054
145.0–200.0	165.90	24007.0	170.9	0.545	43805.8	0.44	0.667	0.004	0.054	0.054
200.0–300.0	228.30	8589.0	56.0	0.496	17183.5	0.12	0.721	0.008	0.060	0.061

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