Adhesion at Diamond /Metal Interfaces: A Density Functional Theory Study

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Adhesion at diamond/metal interfaces: A density functional theory study

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To understand the basic material properties required in selecting a metallic interlayer for enhanced adhesion of diamond coatings on the substrates, the interfaces between diamond and metals with different carbide formation enthalpies (Cu, Ti, and Al) are studied using density functional theory. It is found that the work of separation decreases, while the interface energy increases, with the carbide formation enthalpy \( \Delta H_f \) (Ti < Al < Cu). By comparing the work of separation at the interface with the work of decohesion of the metal, we found that the fracture is more likely to initiate in the metal phase near the interface; therefore a metal phase with a larger surface energy, \( \gamma_s \) (Ti > Cu > Al), is needed to achieve a higher overall interface strength. In addition, when the surface energy is larger than the interface energy, a wetted diamond/metal interface is formed during diamond nucleation, providing the strongest adhesion compared to other growth modes. These results indicate that a strong carbide-forming ability and a large surface energy of the interlayer promote nucleation and enhance the adhesion and interface strength of the coating/substrate system. © 2010 American Institute of Physics. [doi:10.1063/1.3277013]

I. INTRODUCTION

Chemical vapor deposited (CVD) diamond coatings have various applications in many fields, including tribology, mechanics, electronics,1,1 optics,2 and micro-/nanoelectromechanical systems (MEMS/NEMS).3,4 because of their unique properties. However, the broader applications of diamond coatings are hindered by their poor adhesion to substrates. For example, the adhesion failure is a key challenge for integrating diamond films with other materials in diamond-based MEMS/NEMS devices,5 and for using it as the protective coatings in cutting tools that are under high and complicated external stresses during machining. In some electronic devices, metals are deposited on diamonds, where the adhesion of diamond/metal interfaces also influences the electronic contact between metals and the semiconductive diamond.6

The poor adhesion of diamond coatings has been attributed to the high residual stress in the coatings and the weak interfaces between the coatings and substrates. In addition to reducing the residual stresses in diamond coatings,7,8 many efforts, including preseeding, scratching, and adding an interlayer, have been made to enhance the interfacial adhesion of the diamond/metal systems.9 Adding an appropriate interlayer between the diamond coating and substrate can effectively improve the interfacial adhesion.9 The interlayer is expected to serve the following three major functions: (1) as an adhesive layer to enhance the bonding strength of the coating to the substrate, (2) as a diffusion barrier to shield off the detrimental elements such as Co (typically used as a binder for cemented tungsten carbide), which catalyzes diamond to graphite and consequently leads to the coating delamination, and (3) as a nucleation layer to facilitate diamond nucleation and growth in the CVD process. In searching for the best interlayer materials, previous studies suggested that carbide-forming metals (e.g., Ti and Cr) favor diamond nucleation and adhesion more than non-carbide-forming metals (e.g., Cu and Au).9 It is generally believed that the formation of carbides indicates good chemical affinity between the material and carbon, and furthermore, the transition carbide layer provides strong chemical bonds for the diamond coating and the metallic interlayer. However, this theory is difficult to prove due to the lack of quantitative measurements of the true adhesion or interface toughness of diamond/metals. Although different semiquantitative methodologies, which are essentially destructive, have been developed to characterize the adhesion, including Rockwell C indentation,10 scratch,11 superlayer,12 bulge,13 and blister tests,14 the true adhesion energy cannot be precisely measured by experiments. In contrast, accurate atomistic simulation can provide unambiguous inputs for macroscale mechanical modeling.15,16 In this study, we use atomistic computational modeling and simulations to investigate the adhesion of diamond/metal interfaces.

The adhesion of a coating/substrate system is generally expressed in terms of energies to detach the coating from its substrate by an external load.17,18 The energies of detachment include the intrinsic work of adhesion, and extrinsic energies that are associated with dissipative and irreversible processes such as plastic deformation and interface roughness.17,19 The intrinsic work of adhesion is of key importance since many of the irreversible energies can also scale with it.17 This study aims to seek for the connection between the intrinsic interfacial adhesion, which is represented by the ideal work of separation \( W_{sep} \), and the formation enthalpy of the carbide phase \( \Delta H_f \) of a metallic interlayer to provide guide-
lines for the selection for interlayer materials. Here, we take Al, Cu, and Ti as model materials. Of the three model materials, Cu does not form any carbide, while Al and Ti form Al₄C₃ and TiC, respectively. Since Cu has an almost perfect lattice match with diamond, there were many attempts to grow CVD diamond epitaxially on Cu. However, this goal has never been achieved without preseeding diamond on the surface. It was found that an intermediate graphite layer forms on the Cu substrate before diamond nucleates. Surface pretreatments such as carbon implantation and laser-irradiation result in the formation of a graphite interlayer, preventing the epitaxial growth of diamond on Cu. The diamond/Ti interface was found to be tough and adherent.27 No report is found on CVD diamond growth on Al, although Al can form carbides.

The formation of carbides is a spontaneous process in the deposition of diamond by CVD. A sharp diamond/metal interface is seldom observed for carbide-forming metals, in which case the interface region becomes diamond/carbide/metals. It seems unrealistic to model a sharp interface between diamond and metals. However, such a sharp interface keeps the comparison on both carbide-forming and non-carbide-forming metals consistent. In addition, the formation of carbide phases can be suppressed and sharp diamond/metal interfaces can be achieved by depositing metal coatings on diamond substrates at low temperatures using physical vapor deposition for carbide-forming metals. The interfaces between diamond and Cu, Al, and Ti are of interest for diamond-based electronic devices. Epitaxial growth of Cu was reported on clean as well as contaminated diamond surfaces. Al is also used as a gate interfacial layer in diamond field-effect transistors. Theoretical studies using atomically sharp interfaces have confirmed that the interface between contaminated, especially hydrogen-terminated, diamond and Al or Cu is much weaker than clean diamond/Ti. For surface and interface structures, a gamma-phase Ti was reported on clean as well as contaminated diamond. Thus the computed adhesion properties show that cracks can occur inside the TiC phase, but stop at the interface. The interface energy and its correlation with ΔHₙ will be calculated, and then its role in the nucleation of diamond coatings and the implication to the macroscopic adhesion properties will be discussed.

II. COMPUTATIONS

The ab initio calculations are based on the density functional theory (DFT) implemented in the Vienna ab initio simulation package (VASP). In the calculations, the ion-electron interaction is described by projector augmented wave potentials, and the exchange-correlation functional is generalized gradient approximation by Perdew and Wang. The plane-wave energy cutoff is 400.0 eV for all the three diamond/metal interfaces based on convergence tests. For bulk metal calculations, the integration is computed over an 11×11×11 k-point mesh that results in 56 irreducible k-points in the Brillouin zone for fcc Al and Cu, and 96 for hcp Ti. For surface and interface structures, a gamma-centered 8×8×1 mesh is employed and the resultant irreducible k-points in the Brillouin zone are 12 for diamond/Al, 10 for diamond/Cu, and 21 for diamond/Ti interfaces. The positions of atoms are relaxed to minimize the free energy using the conjugate gradient method until the Hellmann-Feynman force on each atom is less than 0.05 eV/Å. The convergence tolerance for the electronic relaxation is 10⁻⁵ eV/Å. The linear tetrahedron method with Blöchl corrections is used to calculate the total energy. More computational details for Al and diamond/Al interfaces have been stated in Ref. As a validation of the computational methodology, all the computed bulk lattice constants are in good agreement with experimental values, within 1.3%. For the three metals selected, the closed packed surfaces are modeled by slabs in vacuum supercells. Every slab has periodic boundary conditions along all the three directions, and the two free surfaces are separated by a 10 Å thick vacuum slab to preclude interactions from image surfaces. All the atoms are allowed to relax. The surface energy is derived by least squares fitting to the total energy as a function of the numbers of layers in the slab. The thickness of each slab is determined through a convergence test. As depicted in Table I, five layers of Al(111), five layers of Cu(111), and four layers of Ti(0002) are sufficient for the surface energy to converge within 0.01 J/m². The calculated Al(111) surface energy, 0.78 J/m², compares well with other DFT results of 0.91 J/m² (Ref. 36) and 0.83 J/m² (Ref. 37) using local density approximation (LDA), and 0.75 J/m² using generalized gradient approximation (GGA). The re-
laxed Cu(111) surface energy, 1.29 J/m², agrees with 1.32 J/m² (Ref. 38) and 1.28 J/m² (Ref. 39) calculated using GGA, 1.585 J/m² using a mixed-basis pseudopotential method.40 and 1.41 J/m² by a full-potential linearized augmented plane-wave (FP-LAPW) method.36 The surface energy of Ti(0001), 1.92 J/m², agrees well with 1.99 J/m² calculated using FP-LAPW (Ref. 36) and 1.96 J/m² by Green function method.41 In short, the calculated surface energies are in good agreement with the reported values calculated by other methodologies, and will be used in the subsequent interface models.

Based on the convergence tests in the surface energy calculations, ten layers of Cu(111) and Al(111), and nine layers of Ti(0002) are selected to form the diamond/metal interface with six bilayers of diamond(111)-1·1·1. In a periodic cell setting without vacuum, each unit cell contains two identical interfaces. For all the interface structures, we choose the interface orientations with the least mismatch strain (less than 1.5%, which was estimated to cause less than ~5% error in the work of separations42). At this level of mismatch, the separation between misfit dislocations in a realistic interface structure is far enough so that the periodic interface is a reasonable approximation.43 The lattice mismatch for diamond and Cu is 1.3%; thus the diamond(111)/Cu(111) interface has one atom per layer in a rhombohedral cell. The common cell length is 2.538 Å after minimizing the stress of the simulation cell. With the compromised lattice, diamond is under 0.6% tensile strain while copper is under 0.7% compressive strain. We have tested interface registries for which Cu atoms are at on-top, bridge, and hollow sites relative to carbon atoms, and found that the on-top registry has the lowest energy. The registry is referred to as diamond(111)(2110)∥Cu(111)(2110). There are 10 Cu and 12 carbon atoms in each unit cell. Due to the large lattice mismatch (14.0% for diamond/Al and 17.0% for diamond/Ti) between the unit cell length of diamond(111) and Ti(0002) or Al(111), a supercell is created to match four carbon atoms in diamond(111) with three Ti atoms in Ti(0002) or three Al atoms in Al(111) per layer, with a rotation of the metal phase by 30° around the common [0001] to reduce the interface mismatch to ~1.3% for diamond(111)/Al(111) and 1.3% for diamond(111)/Ti(0002). The resultant metals (Ti and Al) (0110) overlap with diamond (2110), and the two interfaces are referred to as diamond(111)(2110)∥Ti(0002)(0110) and diamond(111)(2110)∥Al(0002)(0110), respectively. This registry was found to have the lowest energy among other tested registries.31 The unit cell contains 27 Ti and 48 carbon atoms with the compromised cell edge length \(a=b=5.048\) Å for the diamond/Ti model, and 30 Al and 48 carbon atoms with \(a=b=5.027\) Å for the diamond/Al model. In all cases, the interfaces between periodic images are made identical to preclude any dipole moment in the cell.

The interface models are subjected to geometry optimizations and energy minimizations to obtain the equilibrium structures. The average distances at the interfaces are found to be 1.86 Å between diamond and Al, 2.06 Å between diamond and Cu, and 1.94 Å between diamond and Ti. For all the systems, the distances are shorter than the planer distances in equilibrium bulk metals: 2.33 Å for Al(111), 2.10 Å for Cu(111), and 2.32 Å for Ti(0002), respectively. This implies that the interaction between the carbon atoms and the metal atoms may be stronger than that between the metal atoms. More detailed calculation results of the work of separations and analysis to the electronic structure will further confirm this observation, in the Secs. III and IV.

### III. INTERFACE STRENGTH

#### A. Ideal work of separation at the interface

The ideal work of separation is the reversible work required to separate the interface into free surfaces, neglecting plastic and diffusional degrees of freedom. It is defined as

\[
W_{\text{sep}} = \gamma_{1V} + \gamma_{2V} - \gamma_{\text{int}},
\]

where \(\gamma_{1V}\) and \(\gamma_{2V}\) are the surface energies of slabs 1 and 2, respectively; and \(\gamma_{\text{int}}\) is the interface energy. In the slab model, the \(W_{\text{sep}}\) is calculated as \(W_{\text{sep}} = (E_{\text{tot}} + E_{\text{tot}} - E_{12})/A\) where \(E_{\text{tot}}\) is the total energy of constituent slab, \(E_{12}\) is the total energy of the interface system, and \(A\) is the interface area. The shape and volume of the supercell remain the same for separate slabs and the interface system to obtain a consistent comparison.

\(W_{\text{sep}}\) is directly related to the interface toughness. In Griffith fracture theories,44–46 the critical stress \(\sigma_c^G\) for a sharp planar crack of length 2\(c\) is a function of Young’s modulus \(E\) and of the crack resistance \(\gamma_c\) as follows:

\[
\sigma_c^G = \sqrt{\frac{2\gamma_c E'}{\pi c}} = \sqrt{\frac{W_{\text{sep}} E'}{\pi c}},
\]

where \(E' = E/(1-v^2)\) with the Poisson ratio of \(v\). \(\gamma_c\) is usually identified with the free surface energy of the cleavage surface. But for an asymmetric crack at the interface, \(\gamma_c\) is replaced with \(W_{\text{sep}}\). Thus, \(W_{\text{sep}}\) is an indicator of the crack resistance and the toughness of the interface. From Eq. (2) we see a large \(\sigma_c^G\) or \(W_{\text{sep}}\) is desirable for diamond/metal interfaces, such as those in cutting tools that work under large stresses. Table II lists the \(W_{\text{sep}}\) of diamond/Cu, diamond/Ti, and previously calculated diamond/Al interfaces.31 The calculated \(W_{\text{sep}}\) for the diamond/Cu interface, 3.36 J/m², agrees with 3.76 J/m² using the FP-LAPW method, 40 and 3.56 J/m² calculated using DFT method.39

<table>
<thead>
<tr>
<th>System</th>
<th>No. of layers</th>
<th>Surface energy (J/m²)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Al(111)</td>
<td>3</td>
<td>0.75</td>
</tr>
<tr>
<td></td>
<td>5</td>
<td>0.78</td>
</tr>
<tr>
<td>Cu(111)</td>
<td>3–4</td>
<td>1.28</td>
</tr>
<tr>
<td></td>
<td>5–7</td>
<td>1.29</td>
</tr>
<tr>
<td></td>
<td>7–10</td>
<td>1.29</td>
</tr>
<tr>
<td>Ti(0001)</td>
<td>3–7</td>
<td>1.92</td>
</tr>
<tr>
<td></td>
<td>8–9</td>
<td>1.92</td>
</tr>
</tbody>
</table>
method in Ref. 16. The order of $W_{sep}$, ranking from large to small, is diamond/Ti (5.77 J/m$^2$) > diamond/Al (4.08 J/m$^2$) > diamond/Cu (3.36 J/m$^2$). This is consistent with the general belief that carbide-forming metals have better adhesion to diamond coatings than non-carbide-forming metals, although there is no intermediate carbide layer in the sharp diamond/metal interface model.

### B. Bonding nature at the interface

The electron localization function (ELF) (Ref. 47) is employed to explore the interfacial bond character in the three systems. ELF is a localized function of same-spin pairs, which is interpreted either as a spherical average of the Hartree–Fock same-spin pair probability or the excess local kinetic energy due to Pauli exclusion principle. The value of ELF ranges from 0 to 1, where 1 corresponds to the localization as in covalent bonds, and 0.5 corresponds to the electron-gas-like pair probability as in metallic bonds. Topology analysis to ELF can effectively reveal various chemical bonds. Figures 1 and 2 show the ELF contour plots of the three optimized diamond/metal interfaces. The cross sections along the diamond (110) planes that are perpendicular to the interfaces and passing through the supercell origins are shown in Fig. 1. In Fig. 1, atomic positions on the cross sections are marked as well. Notice that atoms at two of every three Al(111) planes and one of every two Ti(0002) atomic planes are not on this cross section. The planes that are parallel to the interfaces and between the diamond and the metal layers are shown in Fig. 2. Figures 2(a)–2(c) also show the projections of the carbon and metal atoms on the interfaces. The interface registry for diamond/Al and diamond/Ti is schematically shown as Fig. 2(d) to assist visualizing the atomic positions and directions. The three Al and Ti atoms in the supercell are numbered, according to their different neighboring carbon atoms: atom 1 is directly on top of the first layer of carbon atom, atom 2 is on the hollow site of the top layer carbon but on top of the second carbon layer, and atom 3 is on top of the hollow set of both the first and the second carbon layers.

Figure 1 shows that covalent bonds (indicated by the regions of red (dark gray) colors) are located between neighboring carbon atoms and between the carbon atoms and the metal atoms at the interfaces. Figure 2 shows that the strongest covalent interfacial bond is between the carbon atom and the metal atom directly atop it. For the diamond/Al and diamond/Ti interfaces, covalent bonds are also formed by sharing the two metal atoms on top of the hollow sites (atoms 2 and 3) with the three underlying carbon atoms. Thus there are two types of covalent bonds at the diamond/Al and diamond/Ti interfaces: (1) the bonds between the carbon atoms and the atop metal atoms, and (2) the bonds between the carbon atoms and the metal atoms on top of the hollow sites. Because of the one-to-one match between diamond(111) and Cu(111), there are only type (1) bonds at the diamond/Cu interface. The contour plots in Fig. 1 indicate that the maximum ELF value at the region between carbon and atop Cu is around 0.7, which is smaller than that between carbon and Al or Ti, about 0.8–0.9. This means that the covalent Cu–C bond is weaker than the Al–C and Ti–C bonds. For the interfaces of diamond/Al and diamond/Ti, the maximum ELF value of type (1) covalent bonds is larger than that of type (2) bonds, which means that type (1) covalent bonds are stronger than type (2). The maximum ELF value of type (1) bonds in diamond/Al is very similar to that in diamond/Ti; both are about 0.9. By carefully examining the contour plots in Fig. 2, we find that the maximum ELF value of type (2) in diamond/Al is about 0.8, slightly lower than that in diamond/Ti, about 0.9. This indicates that the covalent bonds in diamond/Al are weaker than that in diamond/Ti.

<table>
<thead>
<tr>
<th></th>
<th>Diamond/Al</th>
<th>Diamond/Cu</th>
<th>Diamond/Ti</th>
</tr>
</thead>
<tbody>
<tr>
<td>$W_{sep}$ (0/1)</td>
<td>4.08</td>
<td>3.36</td>
<td>5.77</td>
</tr>
<tr>
<td>$W_{dec}$ (1/2)</td>
<td>2.25</td>
<td>2.60</td>
<td>4.01</td>
</tr>
<tr>
<td>$W_{dec}$ (2/3)</td>
<td>1.56</td>
<td>2.60</td>
<td>3.71</td>
</tr>
<tr>
<td>$W_{dec}$ (3/4)</td>
<td>1.60</td>
<td>2.89</td>
<td>3.88</td>
</tr>
<tr>
<td>$\gamma_{int}$</td>
<td>2.45</td>
<td>3.58</td>
<td>1.88</td>
</tr>
</tbody>
</table>

FIG. 1. (Color online) ELF contour plots along diamond (110) plane. The filled gray circles are carbon atoms, and the filled black circles in (a), (b), and (c) are Al, Cu, and Ti atoms, respectively. Note that two Al (111) atomic planes in (a) and one Ti (0002) atomic plane in (c) are not shown because of the rotations of metals to match the diamond (111) plane. Each neighboring color represents a difference of 0.1 in ELF.
From the above analysis to the ELF contour plots, we found that the order of the bond strength at the diamond/metal interface is Ti−C > Al−C > Cu−C, which is consistent with the order of the work of separation at these interfaces. To form a covalent bond at the diamond/metal interfaces, valence electrons must be shared among bonding atoms. Thus, the bond strength can be estimated from the number of the participating valence electrons that form the covalent carbon-metal bonds. Each carbon atom at a diamond surface has only one dangling bond. On the other side, Cu has one valence electron, Al atom has three, and Ti has four. However, for metals, not all the valence electrons are available to form covalent bonds with carbon atoms at the interface, because free electrons are required to maintain the metallic bonds. Therefore, each Cu atom provides less than one valence electron, and a relatively weaker covalent bond with the carbon atom directly below it. Al and Ti can provide one valence electron to develop a stronger covalent bond with carbon atoms directly below them in type (1) bond. In type (2) bonds, each metal atom is shared by 1.5 carbon atoms in average. Thus both Al and Ti can provide enough electrons to form both type (1) and type (2) bonds, while maintaining the metallic bonds with the bulk phase. Since Ti can provide more valence electrons than Al, it develops overall stronger interfacial covalent bonds with carbon atoms than Al. This simple estimation is consistent with the order of interface strengths of the diamond/metal interfaces.

**C. Electronic structure of the weakened metal phase**

The charge density distribution and, even more informatively, the change in the charge density reveal how the interface bonding is formed. The charge density difference is calculated as \( \Delta \rho(\vec{r}) = \rho_{\text{metal}}(\vec{r}) - \rho_{\text{metal}}(\vec{r}) - \rho_{\text{C}}(\vec{r}) \), where the subscripts int, \( M \), and \( C \) stand for the equilibrium interface system, the metal slab, and the diamond slab, respectively. All the atoms are frozen at their equilibrium positions as in the interface models for all the charge density calculations.

As in Fig. 3, the \( \Delta \rho(\vec{r}) \) for the three interfaces are shown as contour plots, where the red (dark gray) regions are for electron gain, and the blue (light gray) for electron loss. Figure 3 shows that the charge density differences, both gain and loss, reach maxima at the interface region. The maximum electron gain is between the metal atom and the carbon atom right below it, corresponding to type (1) bond. In the interfaces of diamond/Al and diamond/Ti, the carbon atoms that have no metal atom on top of them attract electrons from nearby regions to form shared electrons with the metal atoms on the hollow sites, corresponding to type (2) bonds. The charge gain and loss upon the interface formation go beyond the first metal layer into the metal phase. The second layer of Al and Cu and even the third layer of Ti atoms also show some electronic structure change. The charge density differences approach almost zero at the regions about two to three metal layers away from the interfaces.

In addition to the contour plots in Fig. 3, which show the charge density differences on the cross sections that are perpendicular to the interfaces, we also summarize in Fig. 4 the
FIG. 3. (Color online) Contour plots of charge density differences of (a) diamond/Al, (b) diamond/Cu, and (c) diamond/Ti interfaces along the metal (1100) planes. The filled gray circles are carbon atoms, and the filled black circles in (a), (b), and (c) are Al, Cu, and Ti atoms, respectively. Atoms that are not on the sample planes are not shown. The numbers in the bar are in unit of e/Å³.

statistical information (the average and the variance) of the charge density differences on each plane that is parallel to the interface. The average value is the net charge transfer inside or out of the given plane, and the variance represents the inhomogeneity of charge density difference within the plane. From Fig. 4 we see that the averages and variances decrease to about zero at the planes that are two atomic layers away from the interfaces, while fluctuating the most around the interfaces. For the charge density differences at the regions between the first and the second metal layers, the diamond/Al interface has a wavy average and almost zero variance, suggesting an interplanar charge transfer; the diamond/Ti interface shows almost zero average but a peak of variance, suggesting mainly intraplanar charge transfer; and the diamond/Cu interface has both nonzero average and variance, which appears to have the most inhomogeneous charge transfer. As the average and variance approach to about zero beyond the second metal layer, the influence of the diamond/metal interface is expected to extend to the second metal layer, indicating that range of the interface region.

D. The location of fracture interface region

Under an applied load, a fracture may occur right at the interface or inside the bulk phase; thus it is important to compute the work of decohesion, $W_{\text{dec}}$, inside the bulk phase and compare it with $W_{\text{sep}}$ to find out the most vulnerable sites for the fracture in the system. $W_{\text{dec}}$ is defined as the energy difference (per unit surface area) between the fractured system and the interface structure, especially when the fracture occurs inside one phase. When the fracture occurs right at the interface, the same definition is referred to as $W_{\text{sep}}$. The overall strength of the interface region is determined by the weakest link. Because diamond is stronger than metals, only the $W_{\text{dec}}$ inside the metal is compared to $W_{\text{sep}}$ at the interface. If the rupture occurs inside the metal, the $W_{\text{dec}}$ should be simply two times of the surface energy, $2\gamma_s$. However, we have observed apparent deviations when the rupture occurs near the diamond/metal interface. The deviations originated from the chemical interaction at the interface, as observed from the charge transfer analysis in Sec. III C. The charge transfer indicated that the interface is a region that includes at least two atomic layers.

We have calculated the $W_{\text{dec}}$ for the fracture between the first and the second atomic metal layers counted from the interface (represented by $1|2$), between the second and the third $2|3$, and between the third and the fourth $3|4$ metal layers. These values are also listed in Table II, in comparison to $W_{\text{sep}}$ and $2\gamma_s$. For all the three metals, the $W_{\text{dec}}$ is much smaller than $W_{\text{sep}}$, meaning the fracture is more likely to occur inside the metal. It is noted that $W_{\text{dec}} (2|3)$ is the smallest compared to the decohesion energies between other metal layers. There is a difference between Cu and the other two metals. For Cu, the $W_{\text{dec}}$ at $1|2$ and $2|3$ are the same. On the other hand, the $W_{\text{dec}}$ at $1|2$ is larger than $2|3$ by 0.69 and 0.30 J/m² for Al and Ti, respectively. This means that a fracture should initiate between the second and third atomic layers from the diamond/metal interfaces in Al and Ti, but it is possible to start even at the first layer in Cu. Eventually, the $W_{\text{dec}}$ converges to $2\gamma_s$ when the influence of the interface diminishes. The weakening effect on the metal phase near the interface can be attributed to the depletion of electrons from the metal phase to the interface. This weakening effect vanishes at regions that are three atomic layers away from the interface due to the vanishing electronic in-
fluence from the diamond/metal interface. For the overall interface region, the smallest $W_{\text{dec}}$ is smaller, but still close to $2\gamma_s$ of the metal phase. Thus to increase the overall strength of the interface region, a stronger metal with a larger surface energy should be considered.

IV. DEPENDENCE OF $W_{\text{sep}}$ AND $\gamma_{\text{int}}$ ON $\Delta H_f$

The carbide formation ability is indicated by the formation enthalpy of the carbide phase, $\Delta H_f$. The $\Delta H_f$ of the two carbide-forming metals are obtained from literature. It is $-52.4$ kJ/mol for $\text{Al}_4\text{C}_3$ per $\text{Al}$ atom, and $-185.2$ kJ/mol for TiC per Ti atom. The $\Delta H_f$ of the non-carbide-forming metal, Cu, is calculated to be 160.0 kJ/mol per Cu atom using DFT with an imaginary CuC of the NaCl structure. Among all the elements, Ti has the third smallest $\Delta H_f$, which is only larger than that of Hf ($\Delta H_f=-252.4$ kJ/mol) and Zr ($\Delta H_f=-203.7$ kJ/mol). Plotting $W_{\text{sep}}$ versus $\Delta H_f$ in Fig. 5 shows that $W_{\text{sep}}$ decreases with $\Delta H_f$. Since the carbide formation ability also decreases with $\Delta H_f$, the results suggest that large negative $\Delta H_f$ or strong carbide formation ability will improve the strength of the diamond/metal interface.

While $W_{\text{sep}}$ is related to the strength where free surfaces form in fracture, $\gamma_{\text{int}}$ is related to a nucleation process where individual atoms agglomerate on a free surface to form a new interface. $\gamma_{\text{int}}$ is defined as the energy change for the formation of an interface from individual atoms

$$\gamma_{\text{int}} = (E_{\text{tot}}^{\text{sep}} - N_M \mu_M - N_C \mu_C)/A,$$

where $\mu_M$ and $\mu_C$ are the chemical potentials of the metal atoms in the bulk phases and the carbon atoms in diamond, respectively, $N_M$ and $N_C$ are the numbers of corresponding atoms in the system, and $A$ is the interface area. The interface energies are listed in Table II and also plotted versus $\Delta H_f$ in Fig. 5. The calculated interface energy of diamond/Cu, 3.58 J/m$^2$, agrees well with 3.55 J/m$^2$ in Ref. 16. According to Eq. (1), the $\gamma_{\text{int}}$ and $W_{\text{sep}}$ are correlated with each other by the surface energies. $\gamma_{\text{int}}$ increases with $\Delta H_f$ while $W_{\text{sep}}$ decrease with $\Delta H_f$. This conclusion is in general agreement with the empirical model, which links increasing interface energies with increasing formation enthalpies, although that model was proposed mainly for transition metals. The analysis to the relationship between nucleation and $\gamma_{\text{int}}$ will be presented in Sec. V.

V. ENERGETICAL ANALYSIS OF NUCLEATION

By nucleation, the change in Gibbs free energy is

$$\Delta G = V\Delta G_v + A'\gamma_N - A(\gamma_S - \gamma_{\text{int}}),$$

where $V$ is the volume of the nuclei, $\Delta G_v$ is the change in volumetric free energy, $A'$ is the area of the nucleus surface, $A$ is the area of the interface, and $\gamma_S$ and $\gamma_N$ are the surface energies of the substrate and the nuclei, respectively. From Eq. (4) we see that the interface energy $\gamma_{\text{int}}$ is a nucleation barrier. Under a given driving force, the larger the $\gamma_{\text{int}}$ is, the more difficult the nucleation will be. As shown in Fig. 5, $\gamma_{\text{int}}$ increases with $\Delta H_f$, which implies that a substrate with a larger negative $\Delta H_f$ favors the diamond nucleation. This is reasonable because when $\Delta H_f$ is negative, the formation of metal-carbon bonds will release energy and leads to relatively small interface formation energy. The increase in $\gamma_{\text{int}}$ with increasing $\Delta H_f$ also implies that the diamond nucleation is difficult and slow on those substrates with a large positive $\Delta H_f$.

The interface energy ($\gamma_{\text{int}}$) and the surface energies ($\gamma_S$ and $\gamma_N$) are the key parameters in determining the growth mode, which also affects the interface adhesion. The layer-by-layer Frank–van der Merwe growth mode would form a totally wetted interface and provide the strongest adhesion, and it requires $\gamma_S - \gamma_{\text{int}} - \gamma_N > 0$ or $\gamma_{\text{metal}} - \gamma_{\text{diamond}} > \gamma_{\text{int}}$ in our case. Apparently, higher metal surface energy and smaller interface energy favor a better wetting interface to enhance the adhesion, and Ti is the best out of the three metals investigated here. During CVD diamond growth, the growing surface is typically passivated by hydrogen, and the $\gamma_N$ for H terminated diamond (111) is about $-0.03$ J/m$^2$, when the chemical potential of hydrogen is in equilibrium with the source gas of CH$_4$. Based on the surface energies listed in Table I and interface energies listed in Table II, we have that the relationship between $\gamma_{\text{metal}} - \gamma_{\text{diamond}}$ and $\gamma_{\text{int}}$ is $0.75-0.03 < 2.45$ (J/m$^2$) for Al, $1.28-0.03 < 3.58$ (J/m$^2$) for Cu, and $1.92-0.03 > 1.88$ (J/m$^2$) for Ti. Thus, among the three metals, only Ti is possible to form a wetted interface with diamond, evidenced by various experimental data that adherent and tough diamond coatings have been deposited on Ti. In contrast, the negative values of $\gamma_{\text{metal}} - \gamma_{\text{int}} - \gamma_{\text{diamond}}$ on Al and Cu make it difficult to grow adherent diamond coating on the two substrates. To the knowledge of the authors, there is no report on CVD diamond growth on Al. Although the lattice mismatch between diamond and Cu is only 1.3%, there is no epilayer growth of diamond on Cu reported in literature.

Various experiments attempting to deposit diamond on Cu failed, however, various metal phases, including Cu, can easily grow on diamond. If diamond is the substrate, the requirement of $\gamma_{\text{diamond}} - \gamma_{\text{metal}} > \gamma_{\text{int}}$ for the layer-by-layer growth mode is readily fulfilled because the surface energy of bare diamond surfaces without passivation is as high as 5 J/m$^2$. This requirement is satisfied for all the three metals tested here and probably for many other metals. So Cu can be deposited on the diamond substrate, but not the other way around.
VI. SUMMARY

In summary, our study suggests that the smaller formation enthalpy of carbide, $\Delta H_f (\text{Ti} < \text{Al} < \text{Cu})$, and the larger surface energy, $\gamma_s (\text{Ti} > \text{Cu} > \text{Al})$, are required for a metallic interlayer to enhance the adhesion of diamond coatings. The diamond/metal interfaces are strong due to the covalent bonds and the ideal interface strength or the $W_{\text{sep}}$ increases with carbide formation ability, indicated by $\Delta H_f$. Upon the formation of the diamond/metal interface, the change in the electronic structure extends to the second atomic layer inside the metal phase. The electron depletion weakens the metal faces, without considering any carbide phase even on coatings. Although the model uses rather ideal sharp interlayers considered in the present study. Overall, the study is helpful for materials selection of substrates for CVD diamond coatings. Although the model uses rather ideal sharp interfaces, without considering any carbide phase even on carbide-forming substrates, the conclusions are still valid to serve as theoretical limits for the metallic interlayer selection for diamond coatings.

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